

# Example-Guided Synthesis of Relational Queries

---

Aalok Thakkar – Thesis Proposal

December 14, 2022



# Outline

1. Context
2. Timeline
3. Synthesis of Conjunctive Queries
4. Decidability and Complexity Results
5. Extension 1: Union
6. Extension 2: Comparison Predicates
7. Extension 3: Recursion
8. Conclusion and Future Work

# Example-Guided Synthesis of Relational Queries

# Example-Guided Synthesis of Relational Queries

*declarative logic programs*

SQL

Datalog

Cypher

SPARQL

# Example-Guided Synthesis of Relational Queries

*declarative logic programs*

PQL

Prolog

LogiQL

CodeQL

# Example-Guided Synthesis of Relational Queries

*declarative logic programs*

Knowledge Discovery

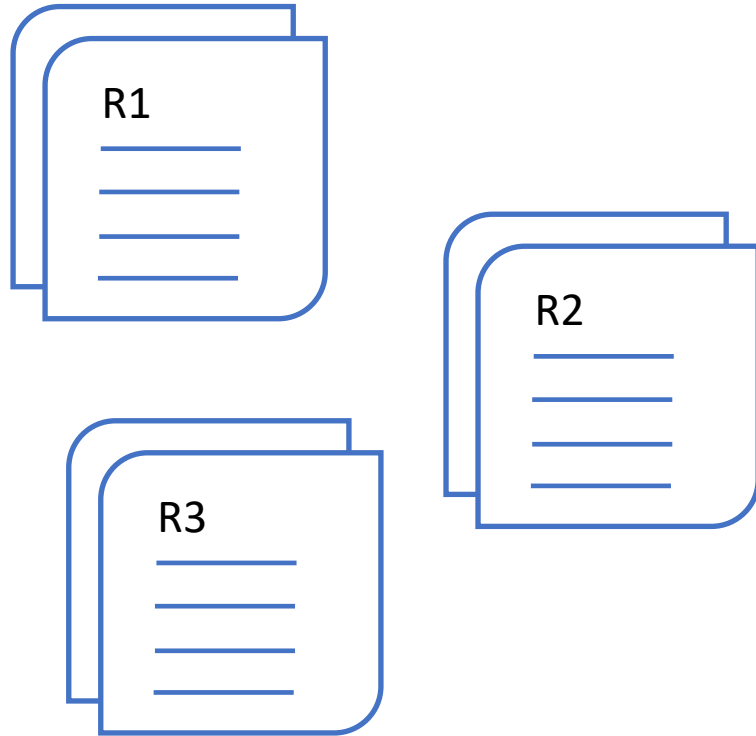
Program Analysis

Database Querying

# Example-Guided Synthesis of Relational Queries

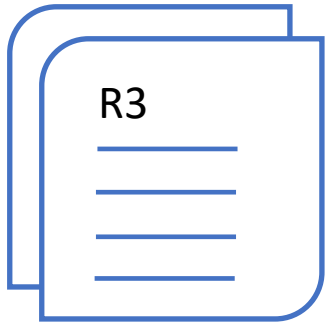
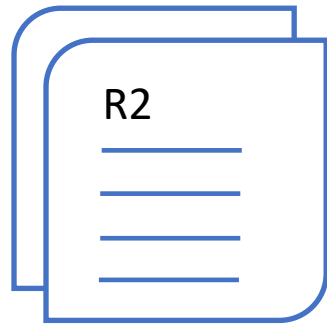
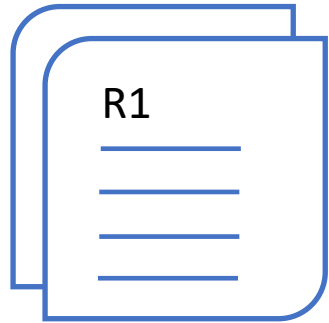


# Query Synthesis Problem



Input Tables

# Query Synthesis Problem

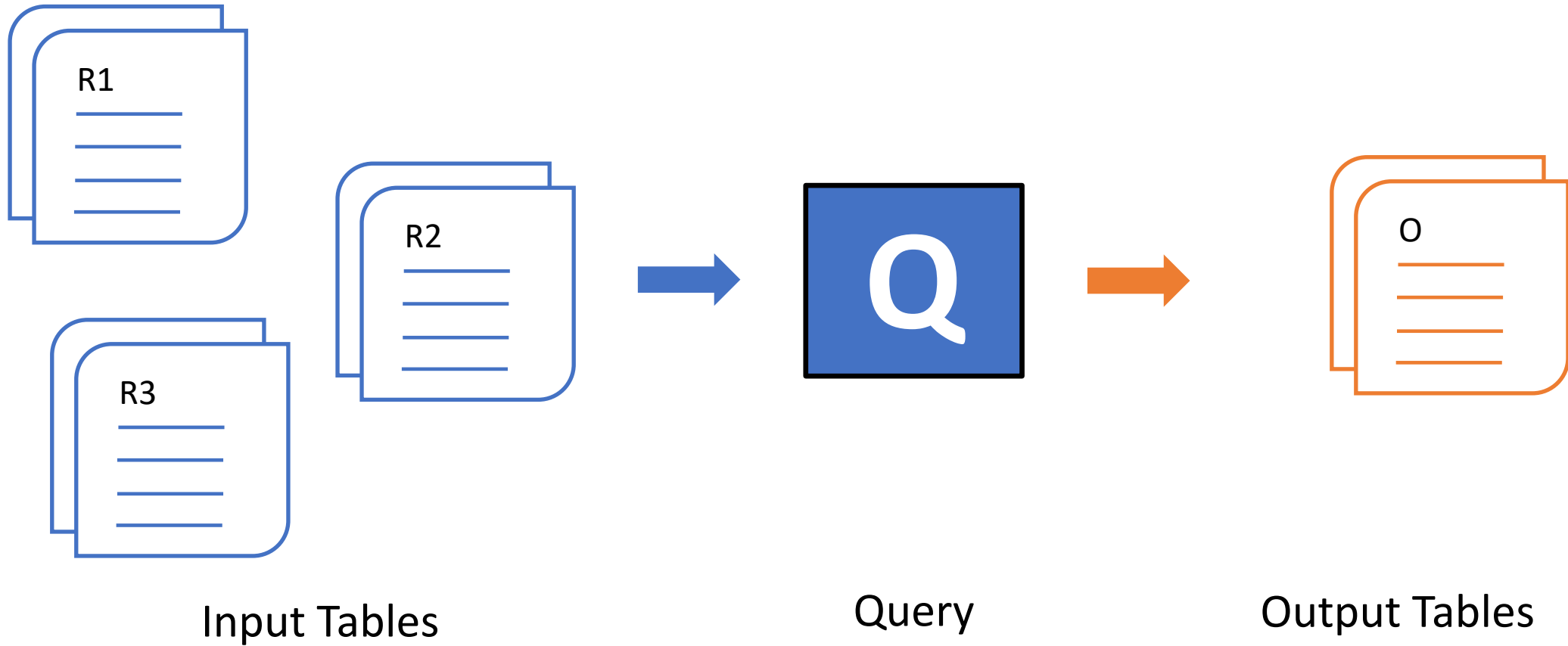


Input Tables

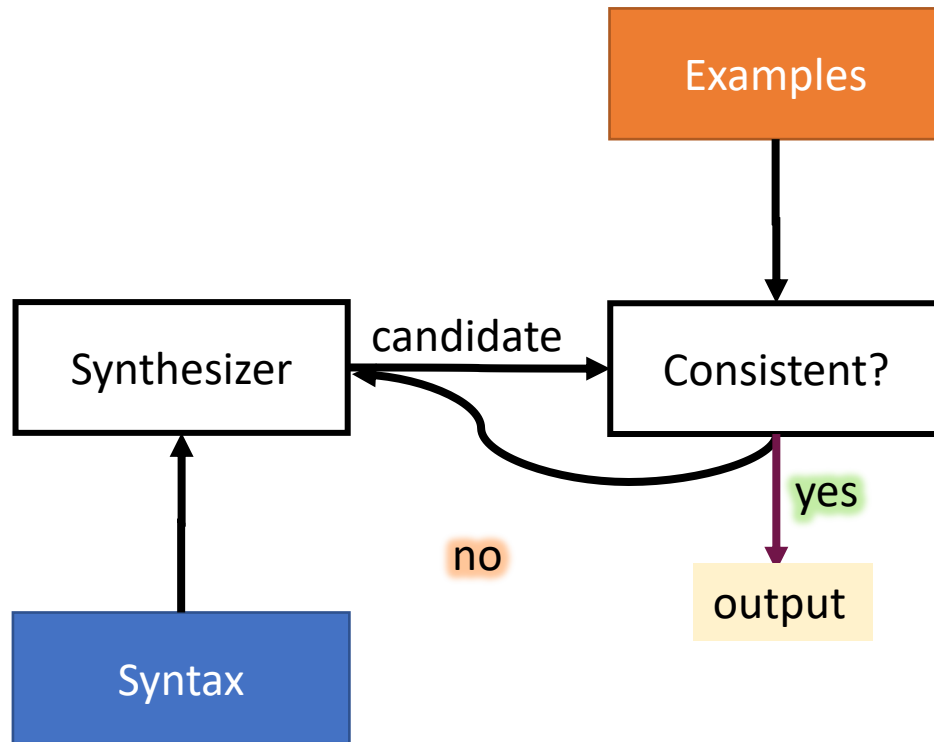


Output Tables

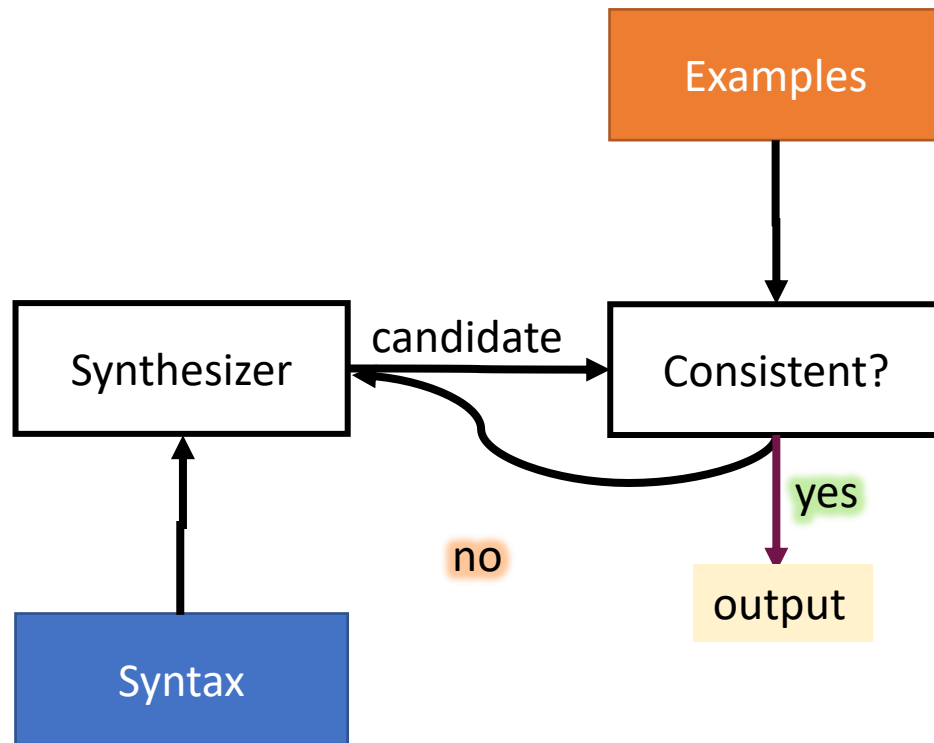
# Query Synthesis Problem



# Syntax-guided Techniques



# Syntax-guided Techniques

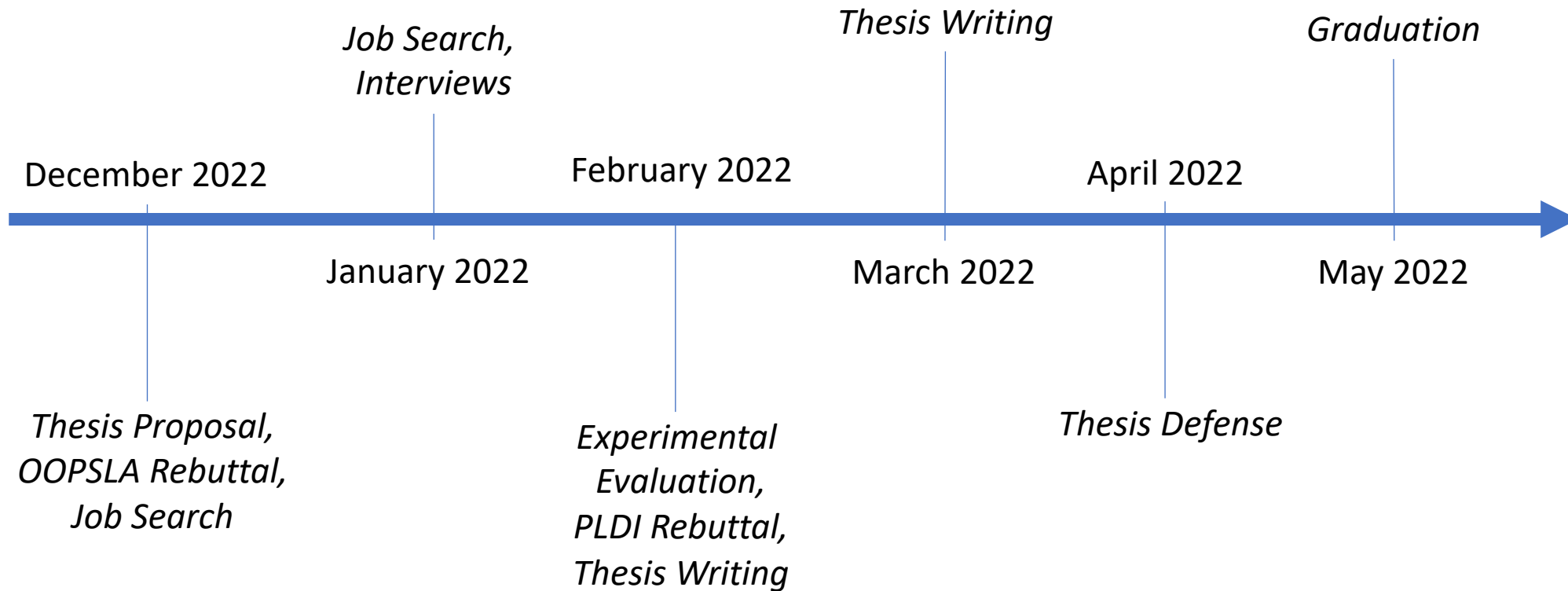


Scythe

Prosynth

ILASP

# Proposed Timeline





# Example-Guided Synthesis of Relational Queries

Aalok Thakkar

University of Pennsylvania  
Philadelphia, USA  
athakkar@cis.upenn.edu

Aaditya Naik

University of Pennsylvania  
Philadelphia, USA  
asnaik@cis.upenn.edu

Nathaniel Sands

University of Southern California  
Los Angeles, USA  
njsands@usc.edu

Rajeev Alur

University of Pennsylvania  
Philadelphia, USA  
alur@cis.upenn.edu

Mayur Naik

University of Pennsylvania  
Philadelphia, USA  
mhnaik@cis.upenn.edu

Mukund Raghothaman

University of Southern California  
Los Angeles, USA  
raghotha@usc.edu

## Abstract

Program synthesis tasks are commonly specified via input-output examples. Existing enumerative techniques for such tasks are primarily guided by program syntax and only make indirect use of the examples. We identify a class of synthesis algorithms for programming-by-examples, which we call Example-Guided Synthesis (EGS), that exploits latent structure in the provided examples while generating candidate programs. We present an instance of EGS for the synthesis of relational queries and evaluate it on 86 tasks from three application domains: knowledge discovery, program analy-

## 1 Introduction

Program synthesis aims to automatically synthesize a program that meets user intent. While the user intent is classically described as a correctness specification, synthesizing programs from input-output examples has gained much traction, as evidenced by the many applications of programming-by-example and programming-by-demonstration, such as spreadsheet programming [25], relational query synthesis [51, 57], and data wrangling [19, 33]. Nevertheless, their scalability remains an important challenge, and often hinders their application in the field [5].

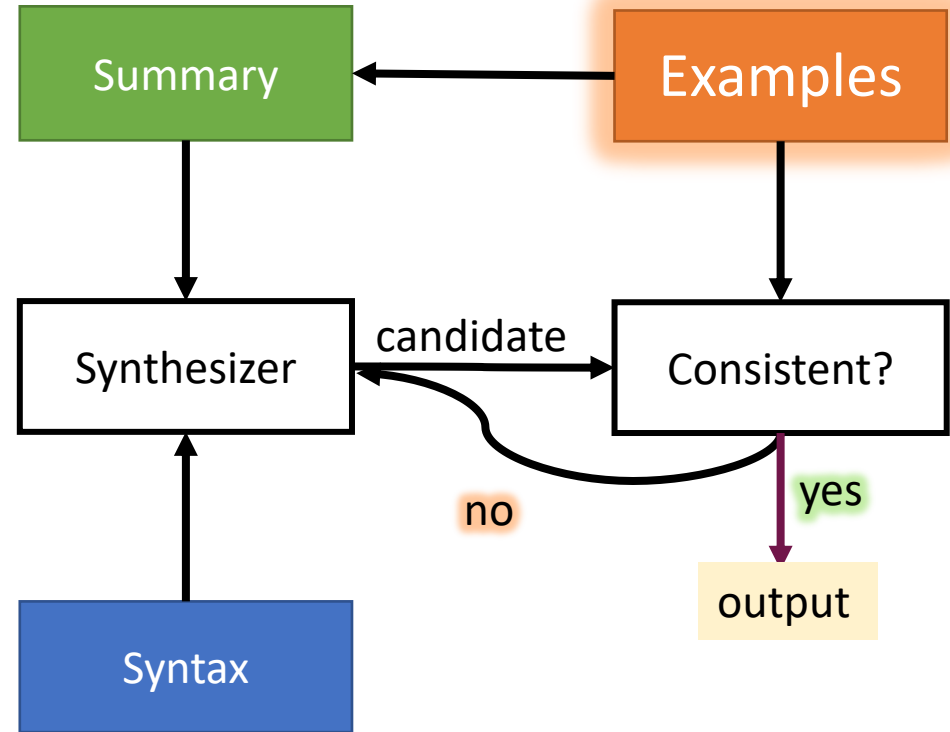
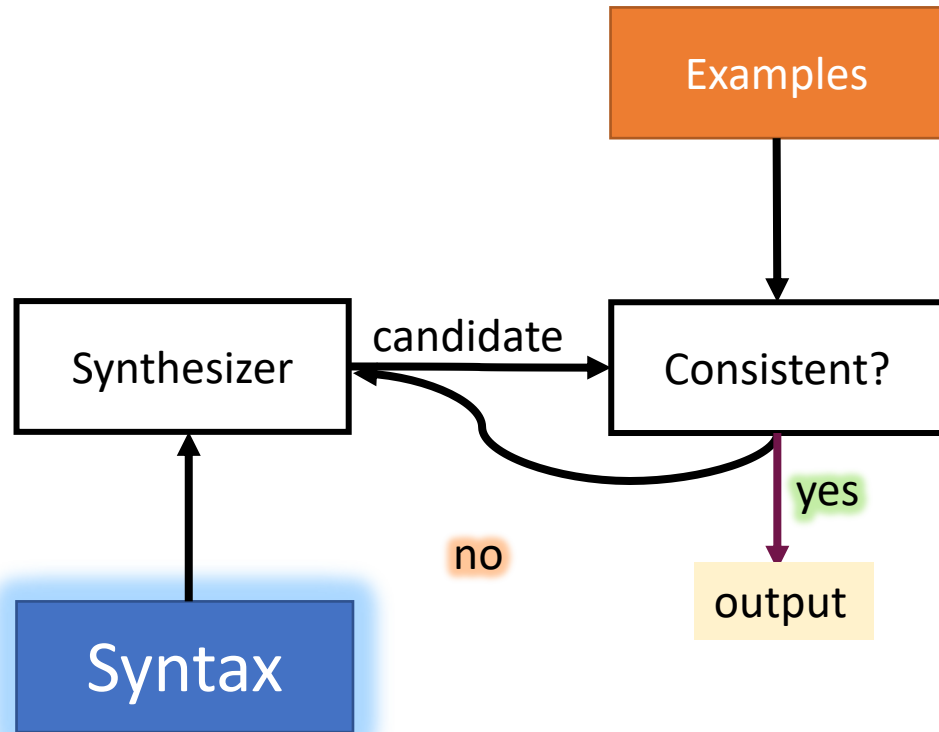
# Example-Guided Synthesis of Relational Queries



# Example-guided Synthesis

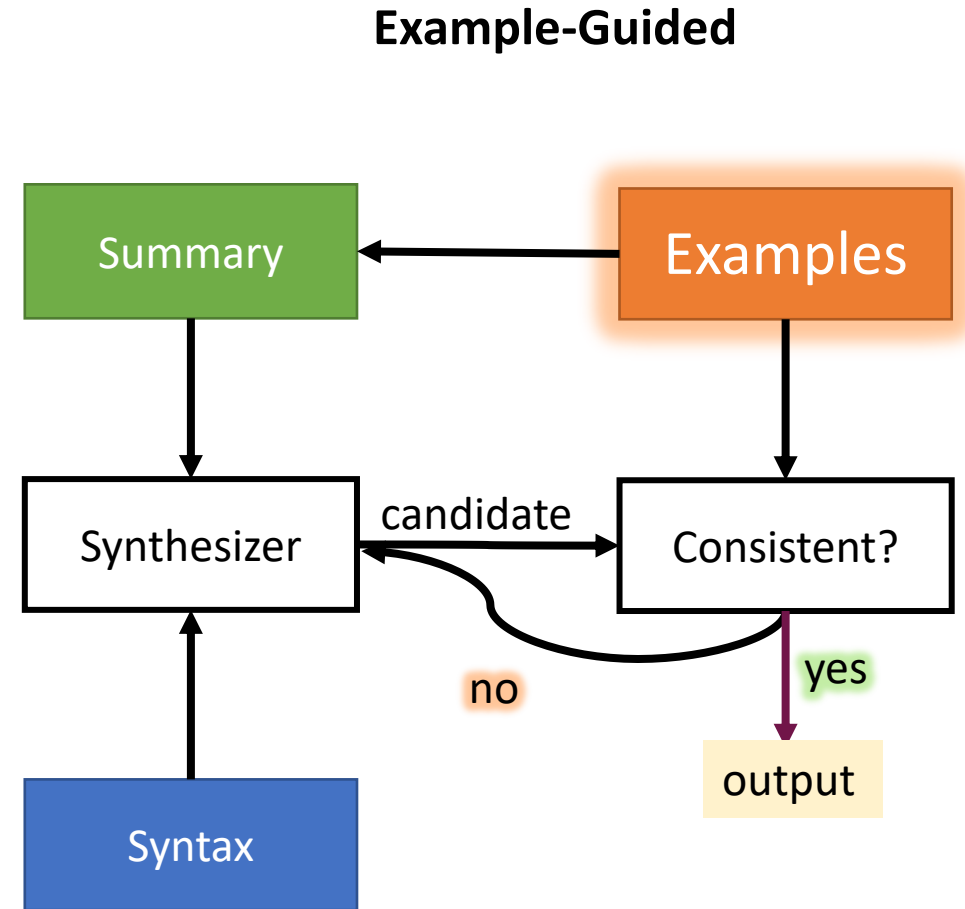
Syntax-Guided

Example-Guided



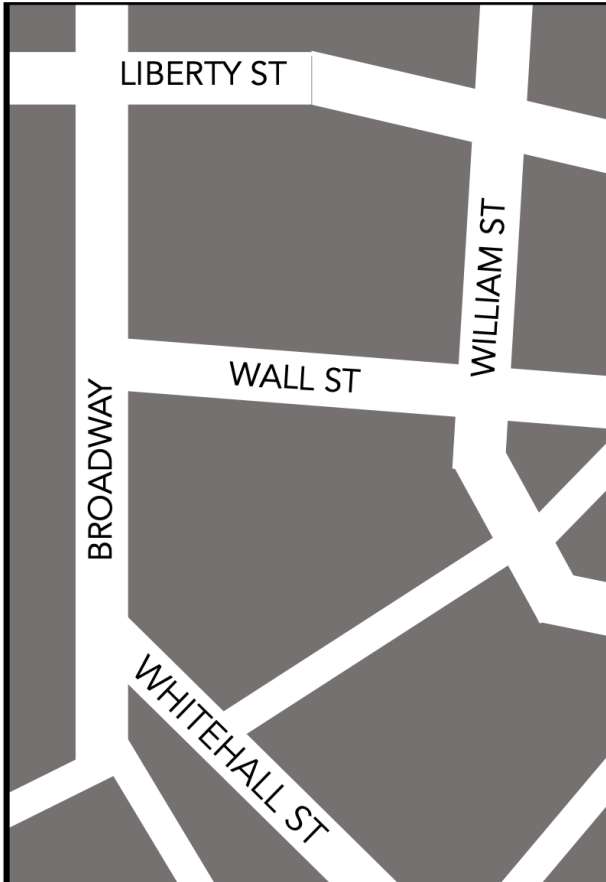
# Example-guided Synthesis

1. Examples cannot be replaced by an evaluation oracle
2. Uses the latent *structure* of examples to generate the candidate programs
3. Outperforms syntax-guided techniques for relational queries



# Example-Guided Synthesis of Relational Queries

# An Example



## **GreenSignal**

---

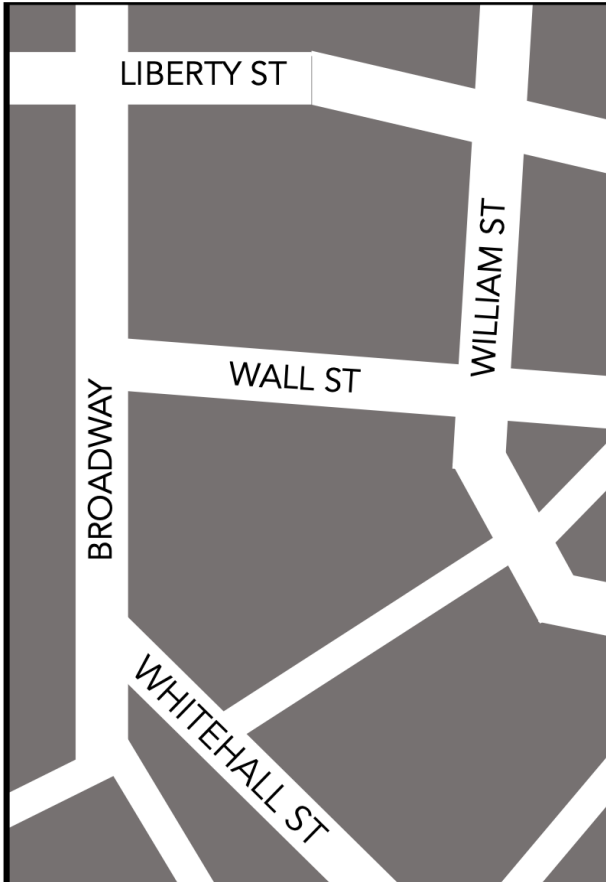
Broadway  
Liberty St  
William St  
Whitehall St

## **HasTraffic**

---

Broadway  
Wall St  
William St  
Whitehall St

# An Example



## GreenSignal

Broadway  
Liberty St  
William St  
Whitehall St



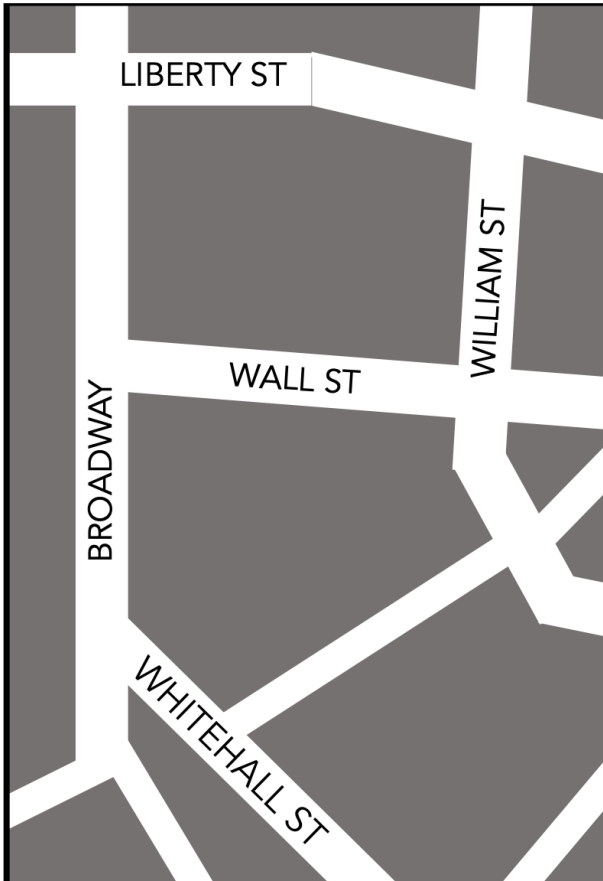
## Crashes

Broadway  
Whitehall St

## HasTraffic

Broadway  
Wall St  
William St  
Whitehall St

# An Example



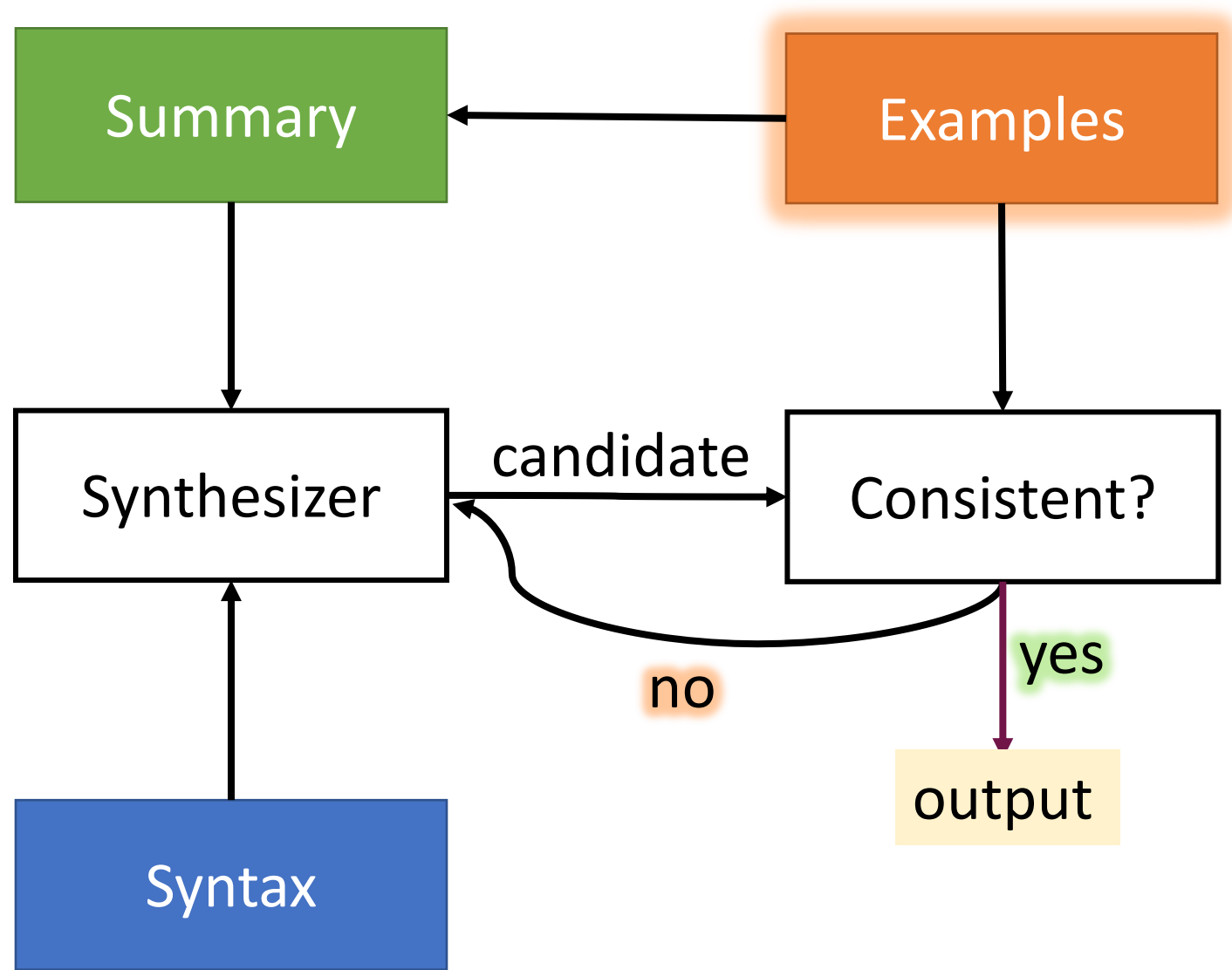
## **GreenSignal**

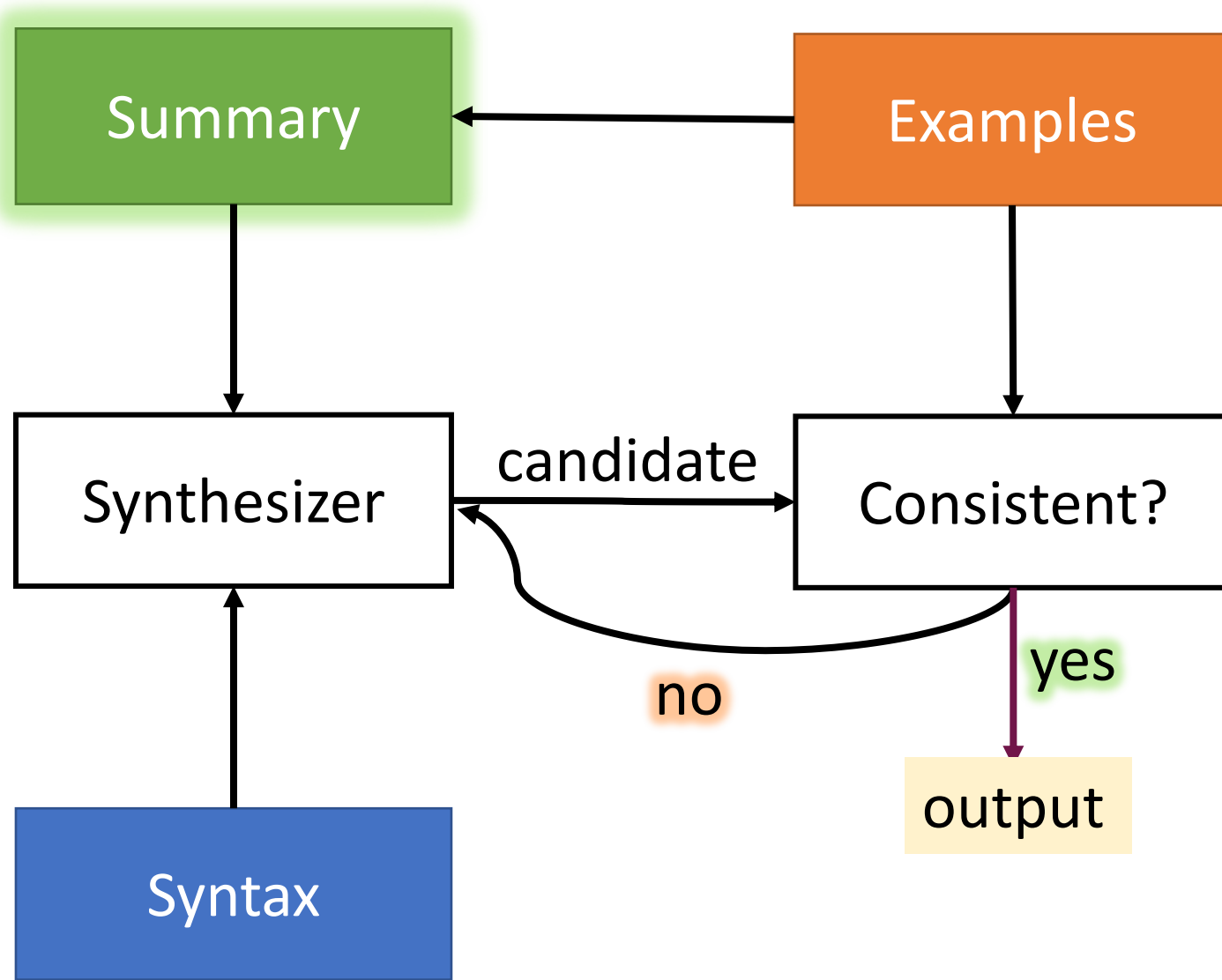
Broadway  
Liberty St  
William St  
Whitehall St

## **HasTraffic**

Broadway  
Wall St  
William St  
Whitehall St

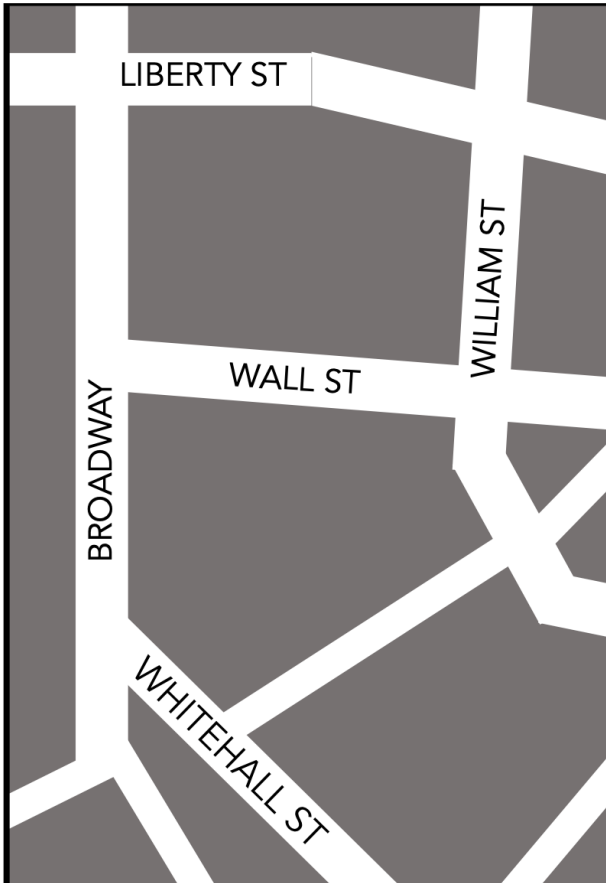
Crashes(x) :  $\neg$  HasTraffic(x).  
Crashes(x) :  $\neg$  GreenSignal(x).  
Crashes(x) :  $\neg$  Intersects(x, y).  
Crashes(x) :  $\neg$  Intersects(y, x).  
Crashes(x) :  $\neg$  HasTraffic(x), GreenSignal(x).  
Crashes(x) :  $\neg$  HasTraffic(x), Intersects(x, y).  
Crashes(x) :  $\neg$  HasTraffic(x), Intersects(y, x).  
Crashes(x) :  $\neg$  GreenSignal(x), Intersects(x, y).  
Crashes(x) :  $\neg$  GreenSignal(x), Intersects(y, x).  
Crashes(x) :  $\neg$  Intersects(x, y), Intersects(y, x).  
Crashes(x) :  $\neg$  HasTraffic(x), GreenSignal(x),  
Intersects(x, y).  
Crashes(x) :  $\neg$  HasTraffic(x), GreenSignal(y),  
Intersects(y, x).  
...







# An Example

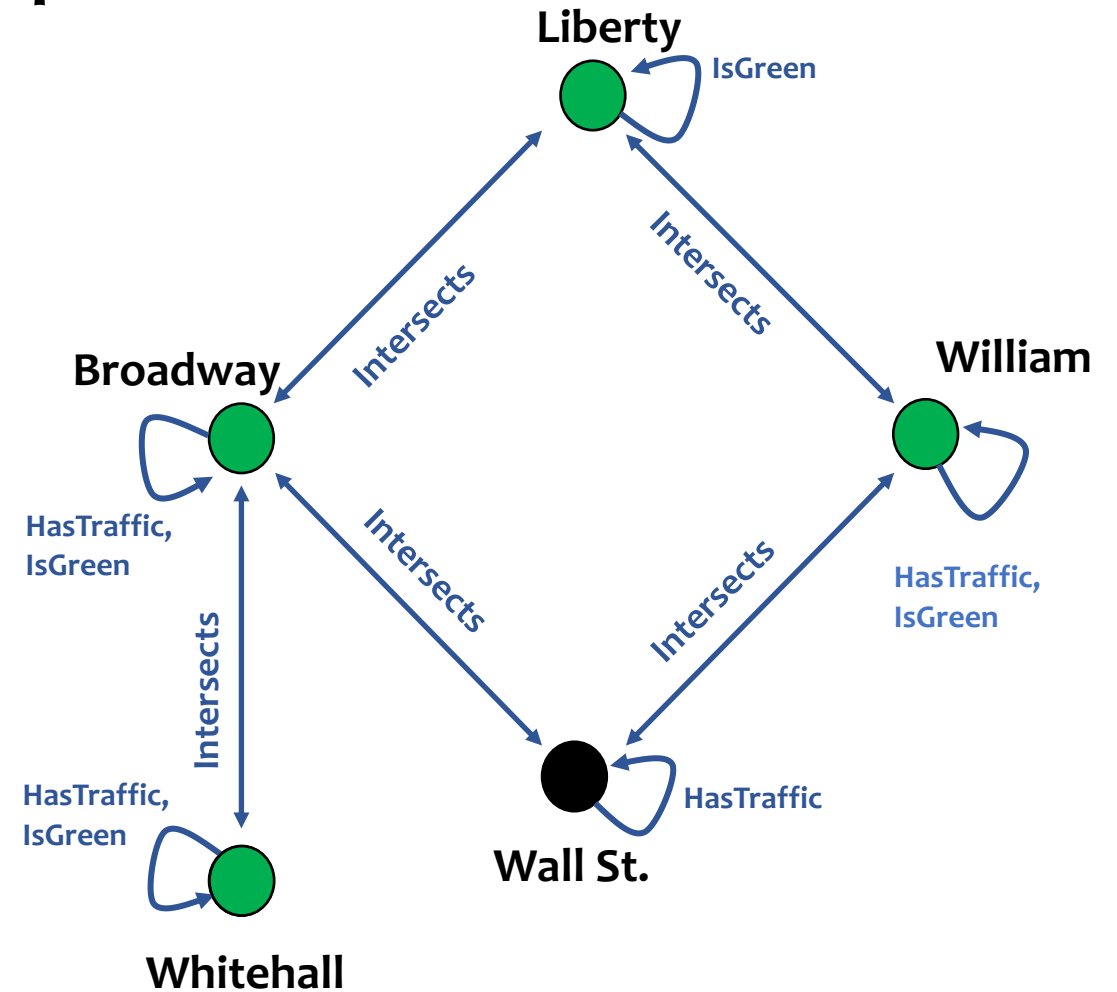


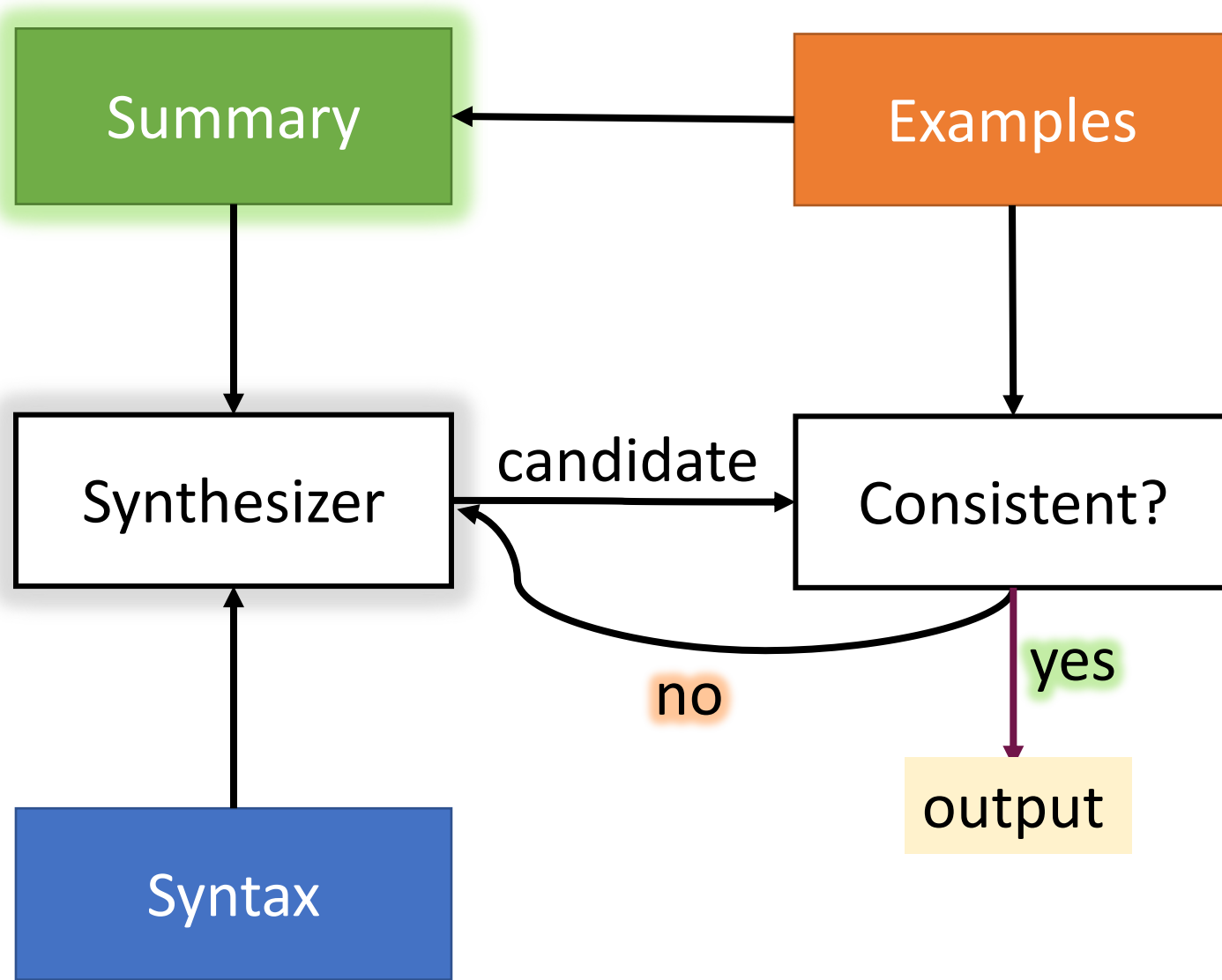
## GreenSignal

Broadway  
Liberty St  
William St  
Whitehall St

## HasTraffic

Broadway  
Wall St  
William St  
Whitehall St



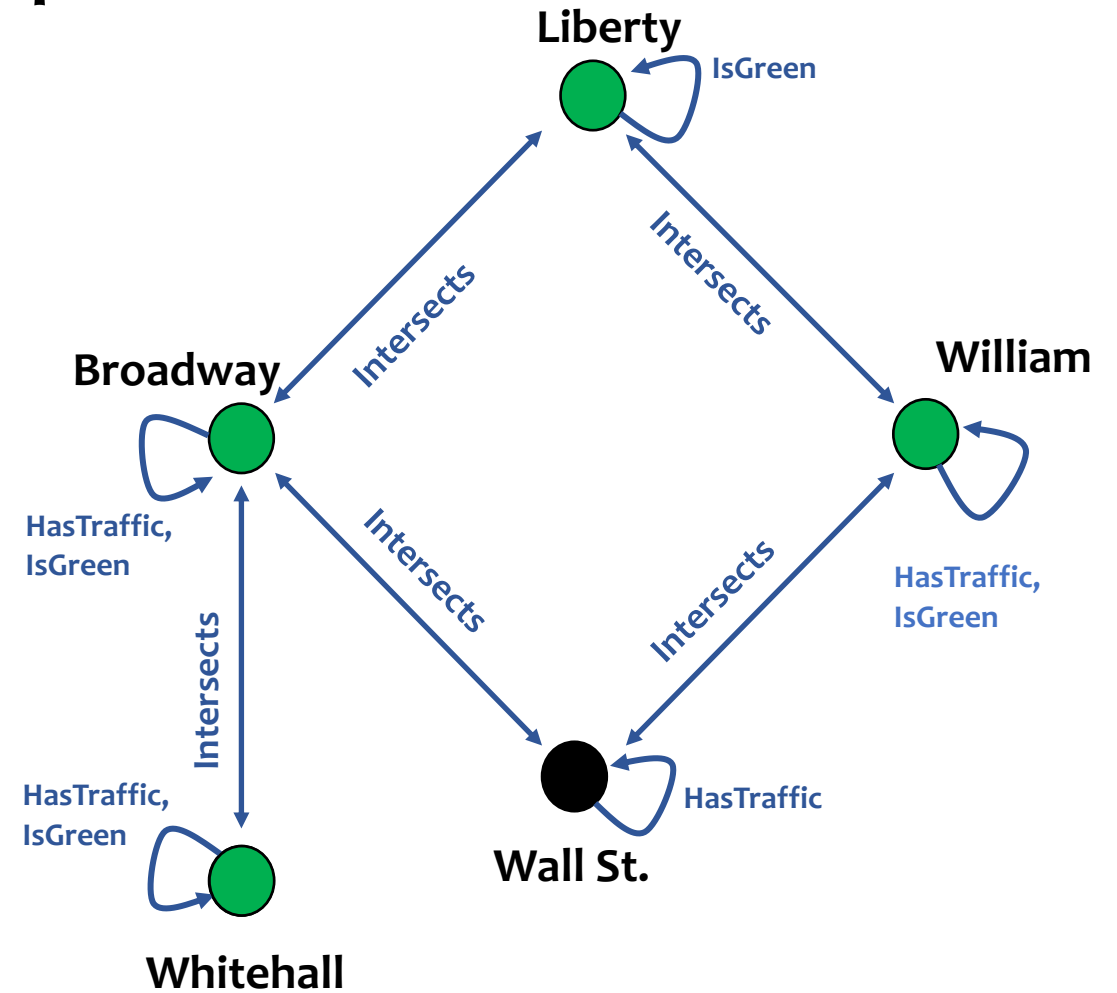


# An Example

## Crashes

Broadway

Whitehall St

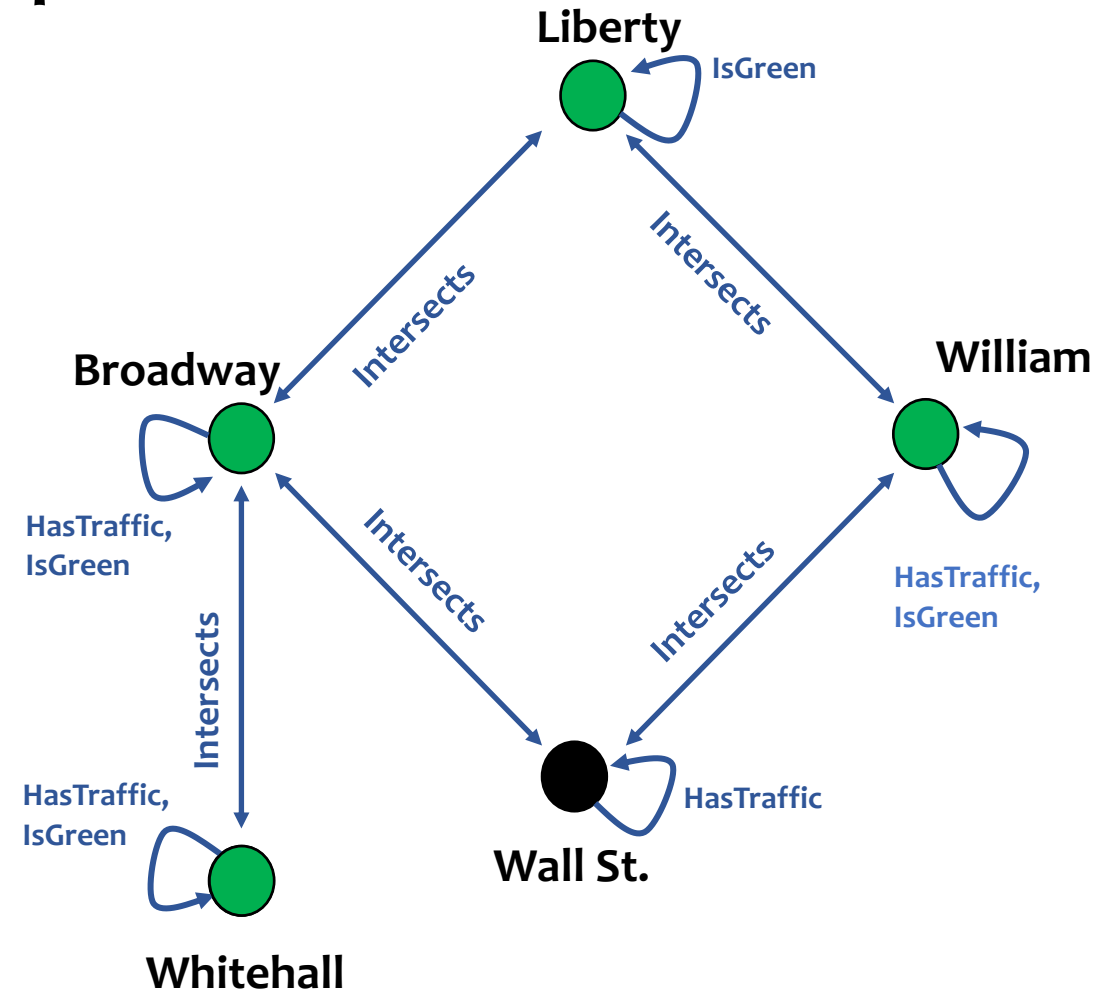


# An Example

## Crashes

Broadway

Whitehall St

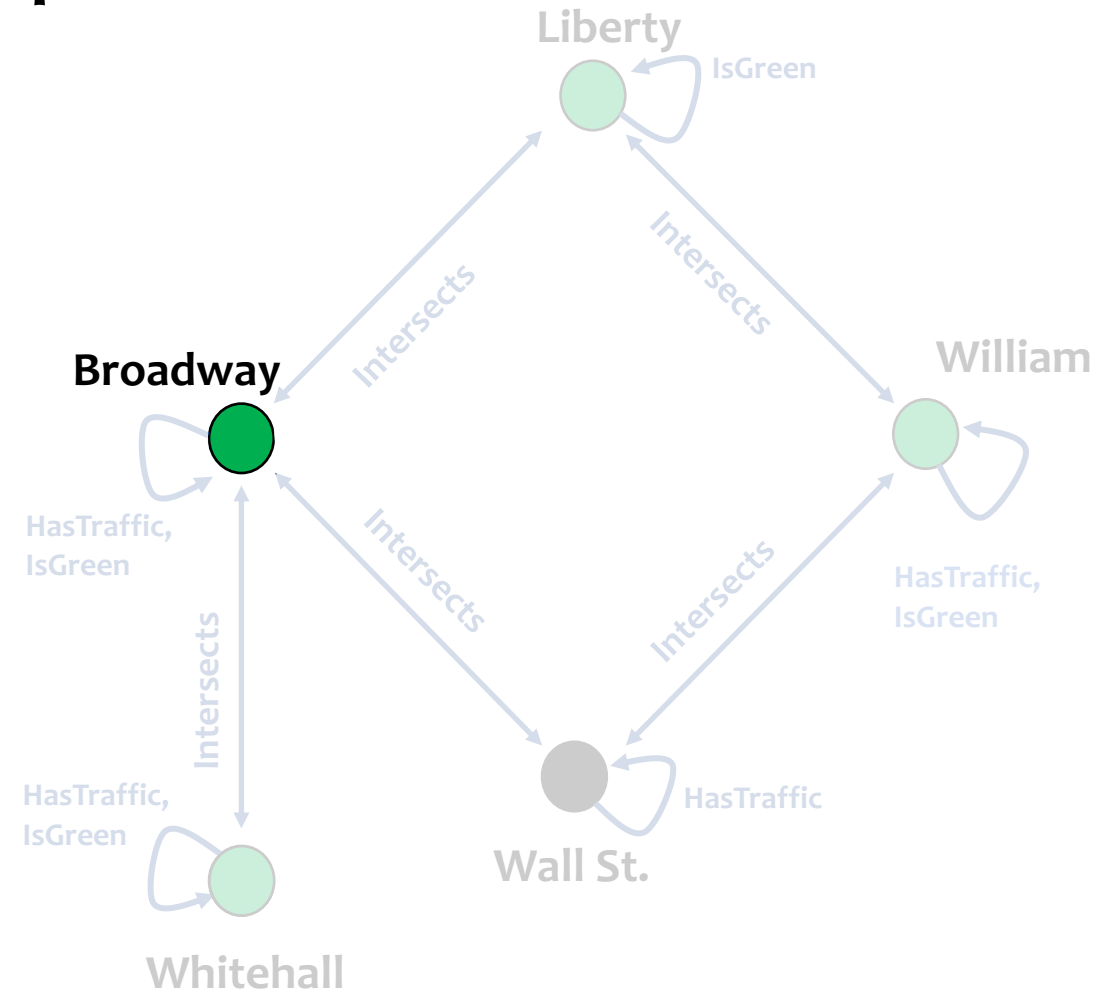


# An Example

## Crashes

Broadway

Whitehall St



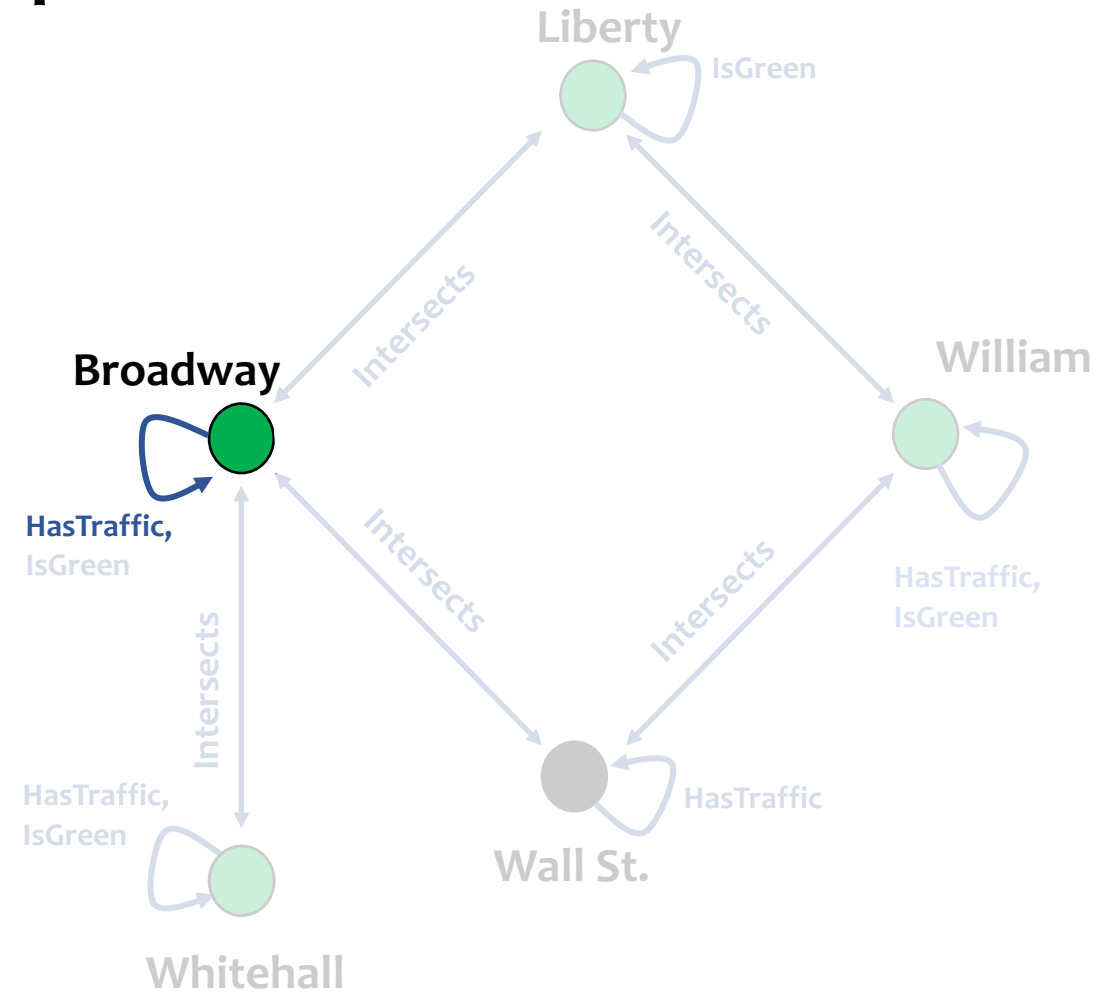
# An Example

## Crashes

Broadway

Whitehall St

Crashes(Broadway)  $\leftarrow$  HasTraffic(Broadway).



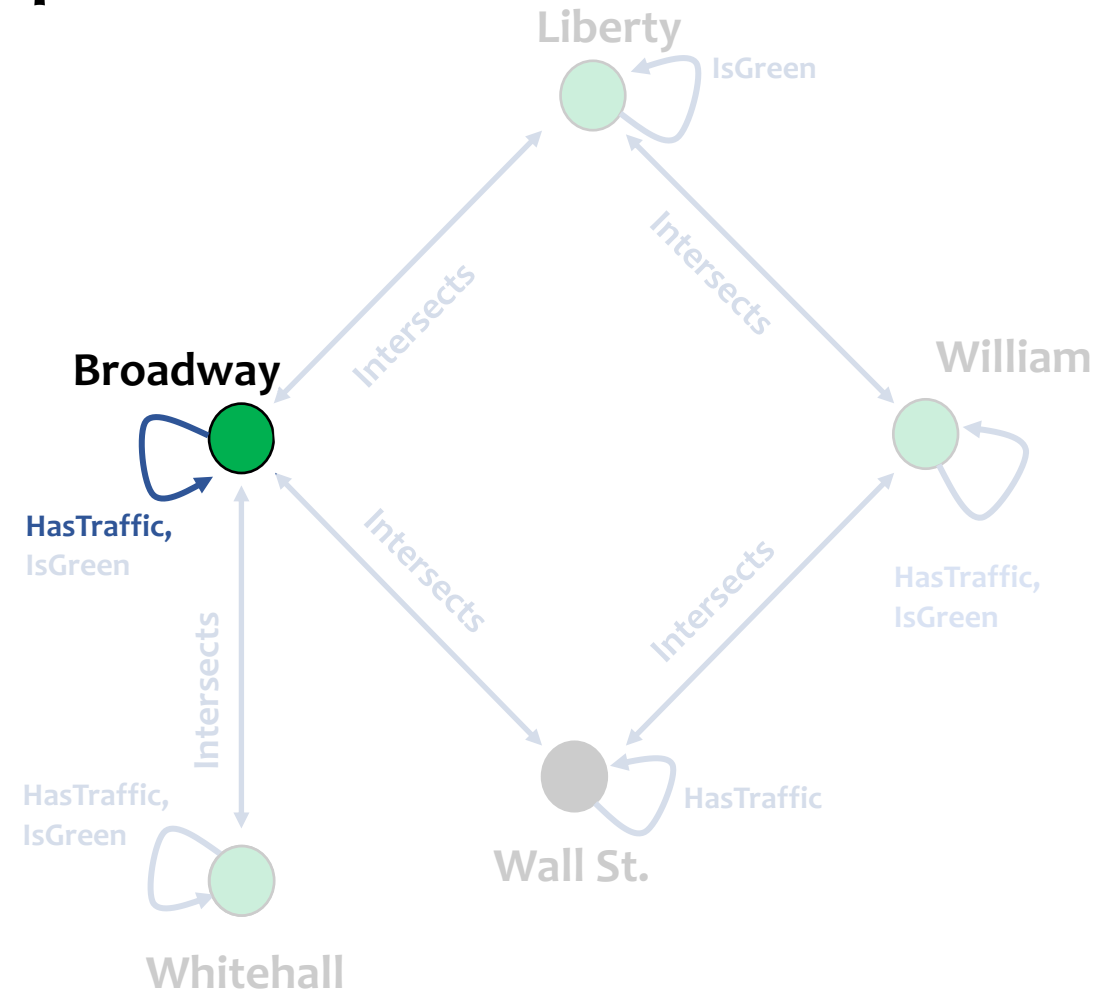
# An Example

## Crashes

Broadway

Whitehall St

Crashes(Broadway) :  $\neg \text{HasTraffic}(\text{Broadway})$ .



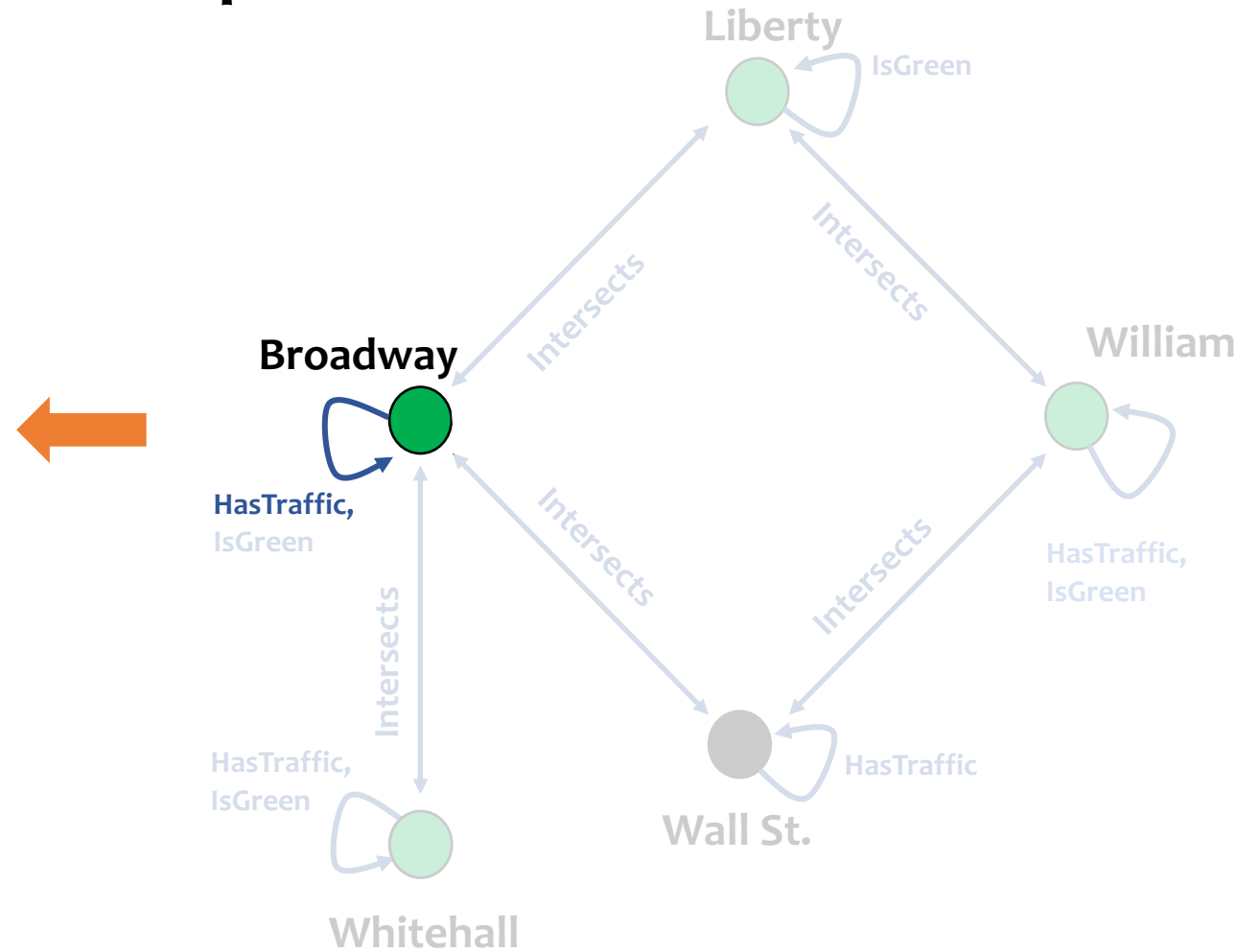
# An Example

## Crashes

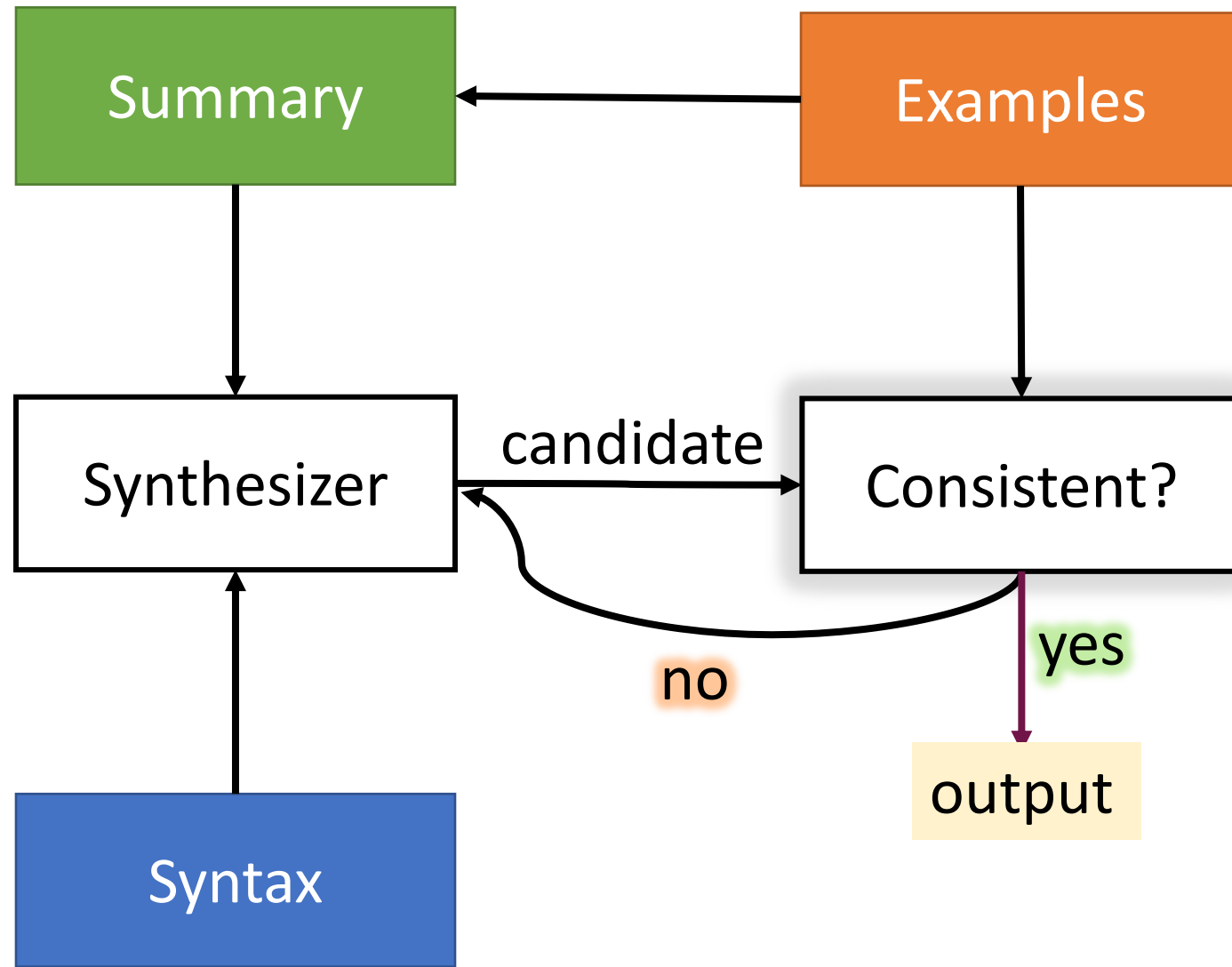
Broadway

Whitehall St

$\text{Crashes}(x) : \neg \text{HasTraffic}(x).$







# An Example

## Crashes

Broadway

Whitehall St

$\text{Crashes}(x) : \neg \text{HasTraffic}(x).$

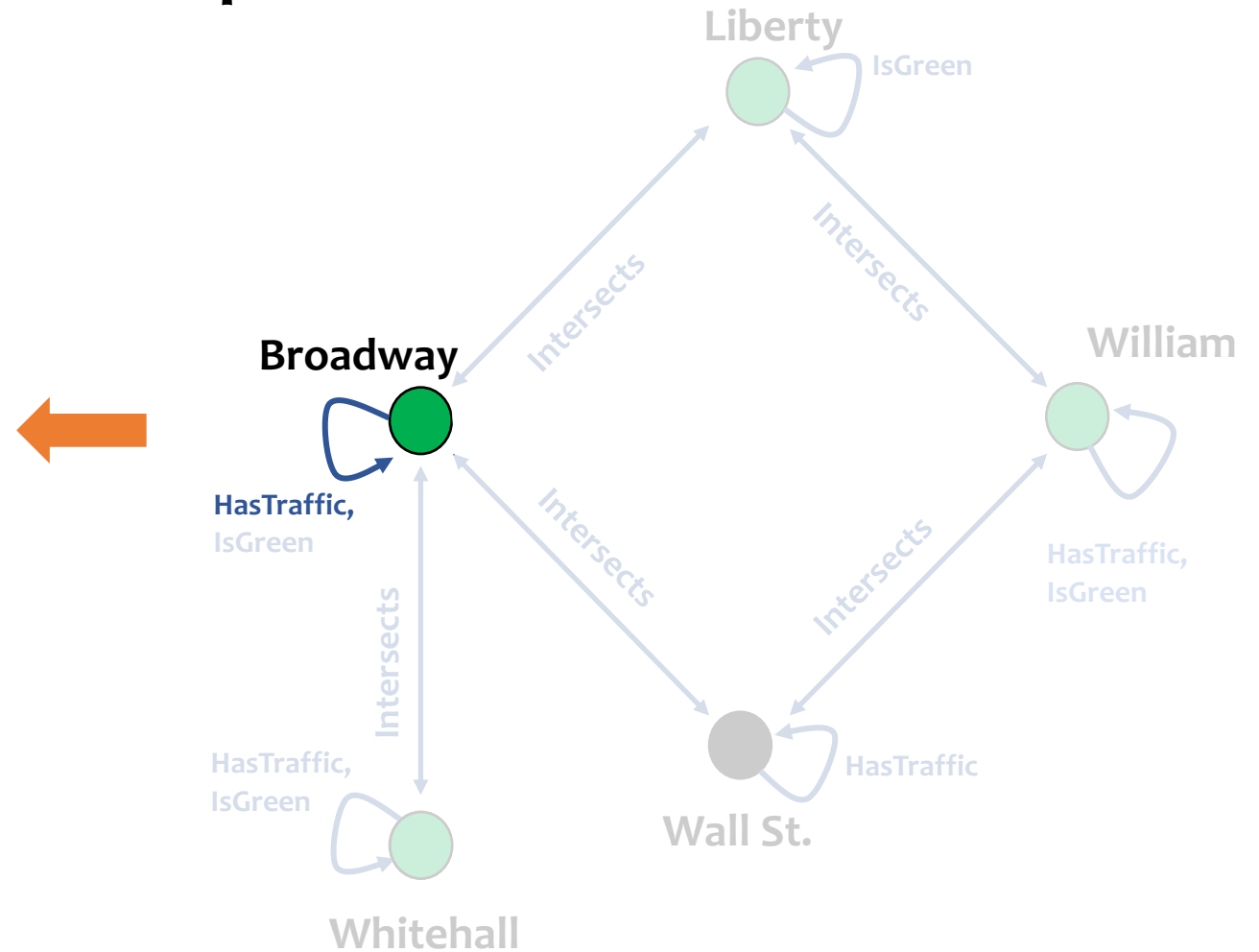
## Crashes

Broadway

Wall St

William St

Whitehall St



# An Example

## Crashes

Broadway

Whitehall St

$\text{Crashes}(x) : \neg \text{HasTraffic}(x).$

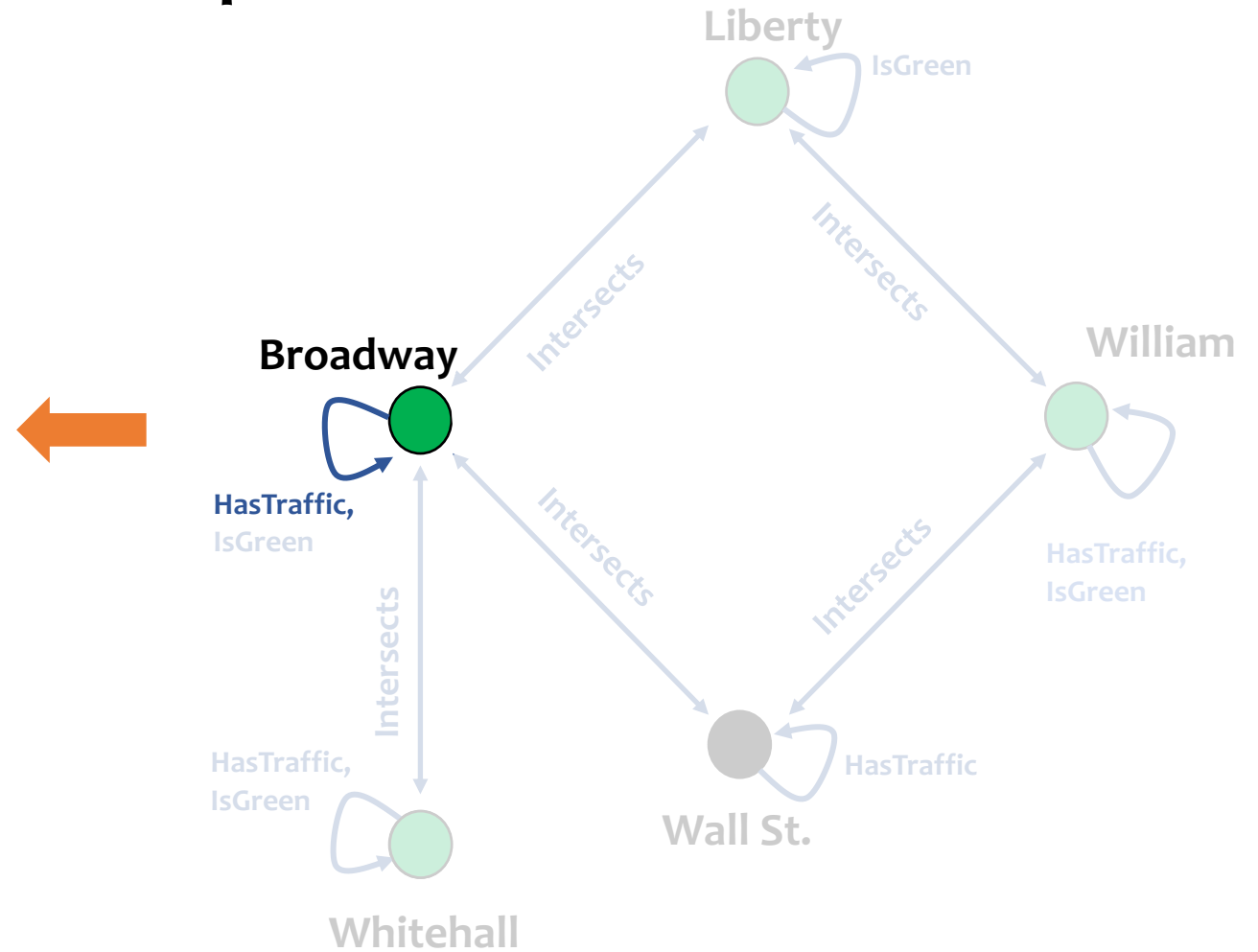
## Crashes

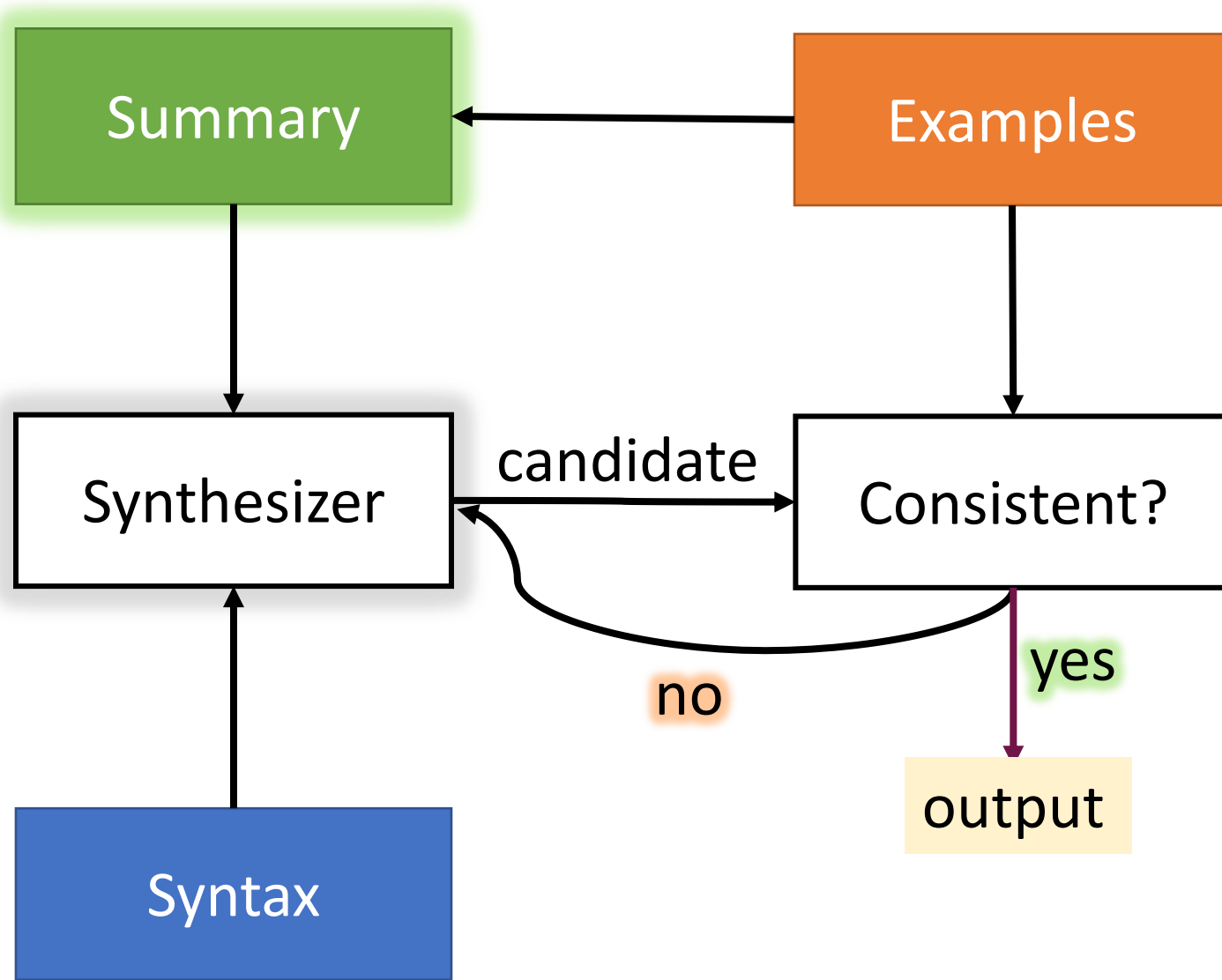
Broadway

Wall St

William St

Whitehall St





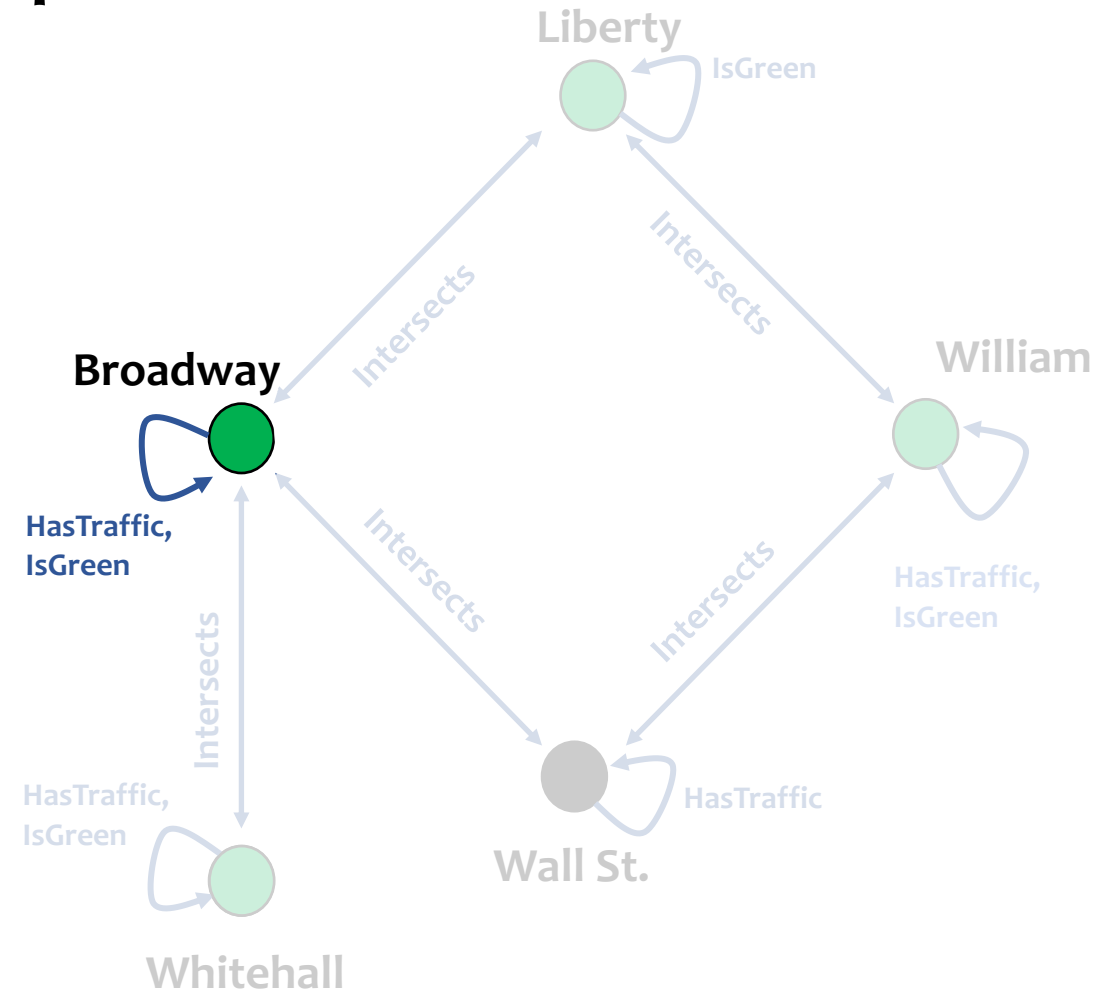
# An Example

## Crashes

Broadway

Whitehall St

$\text{Crashes}(x) : \neg \text{HasTraffic}(x), \text{isGreen}(x).$



# An Example

## Crashes

Broadway

Whitehall St

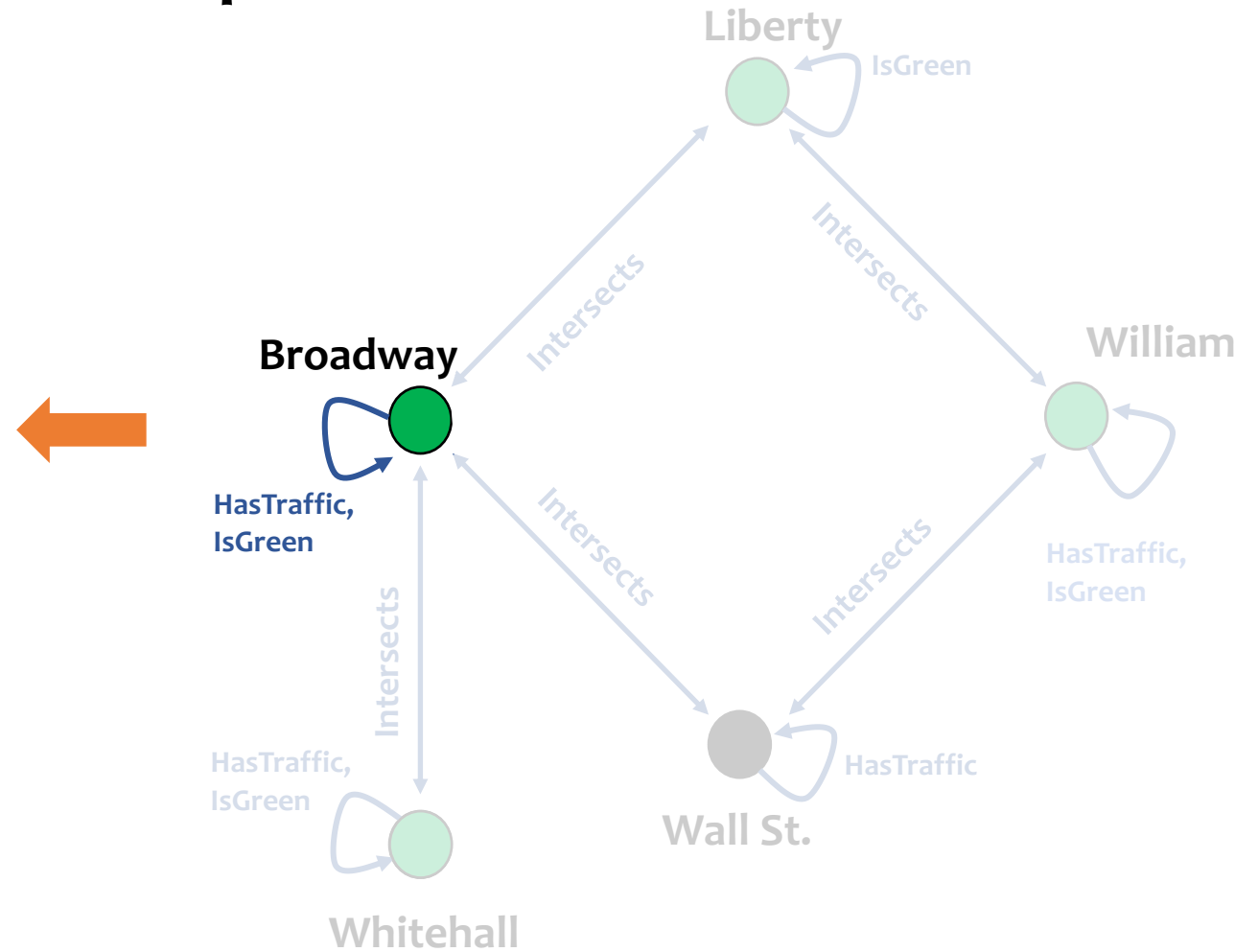
$\text{Crashes}(x) : \neg \text{HasTraffic}(x), \text{isGreen}(x).$

## Crashes

Broadway

William St

Whitehall St



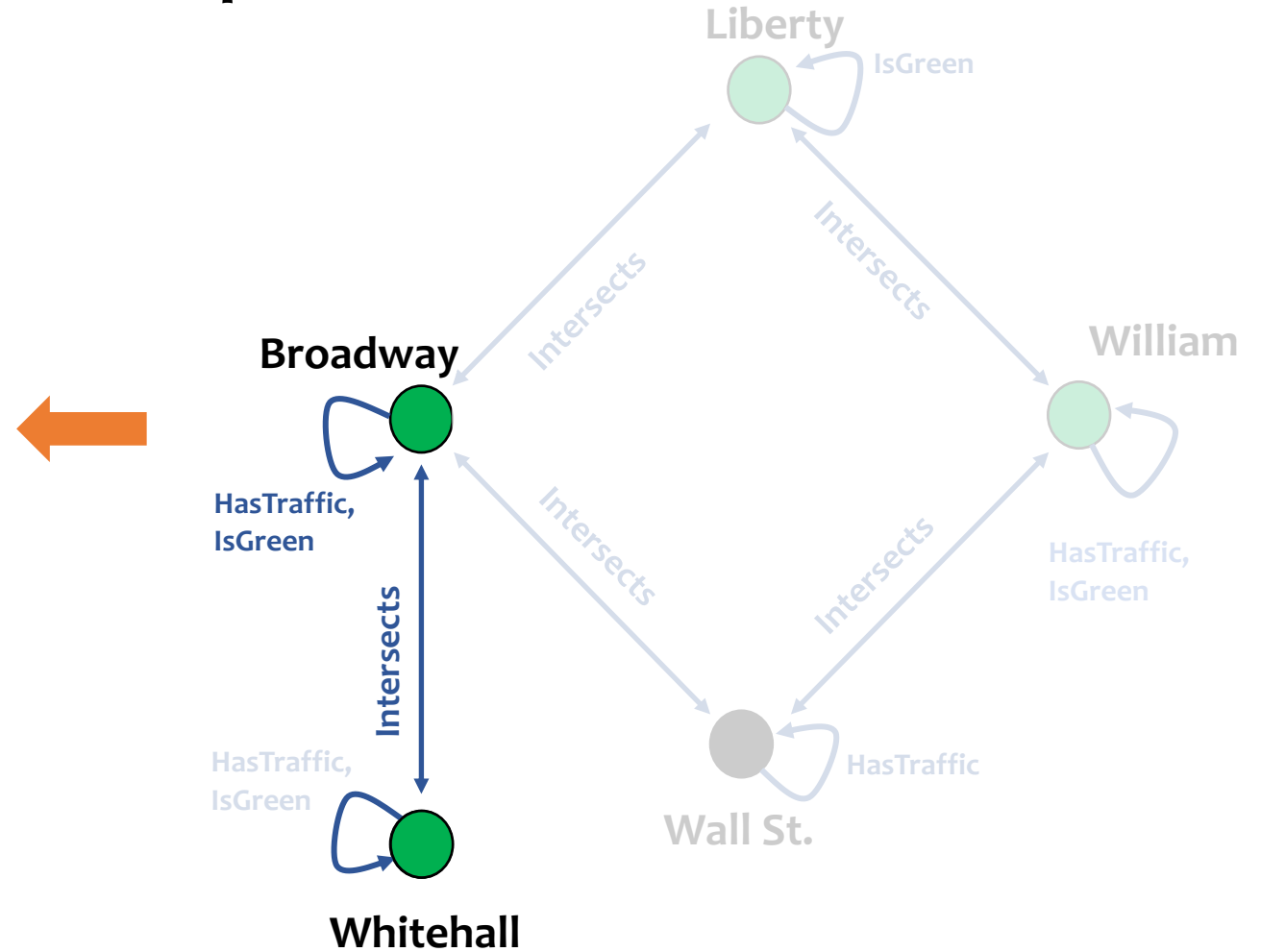
# An Example

## Crashes

Broadway

Whitehall St

$\text{Crashes}(x) : \neg \text{HasTraffic}(x), \text{isGreen}(x), \text{Intersects}(x, y).$



# An Example

## Crashes

Broadway

Whitehall St

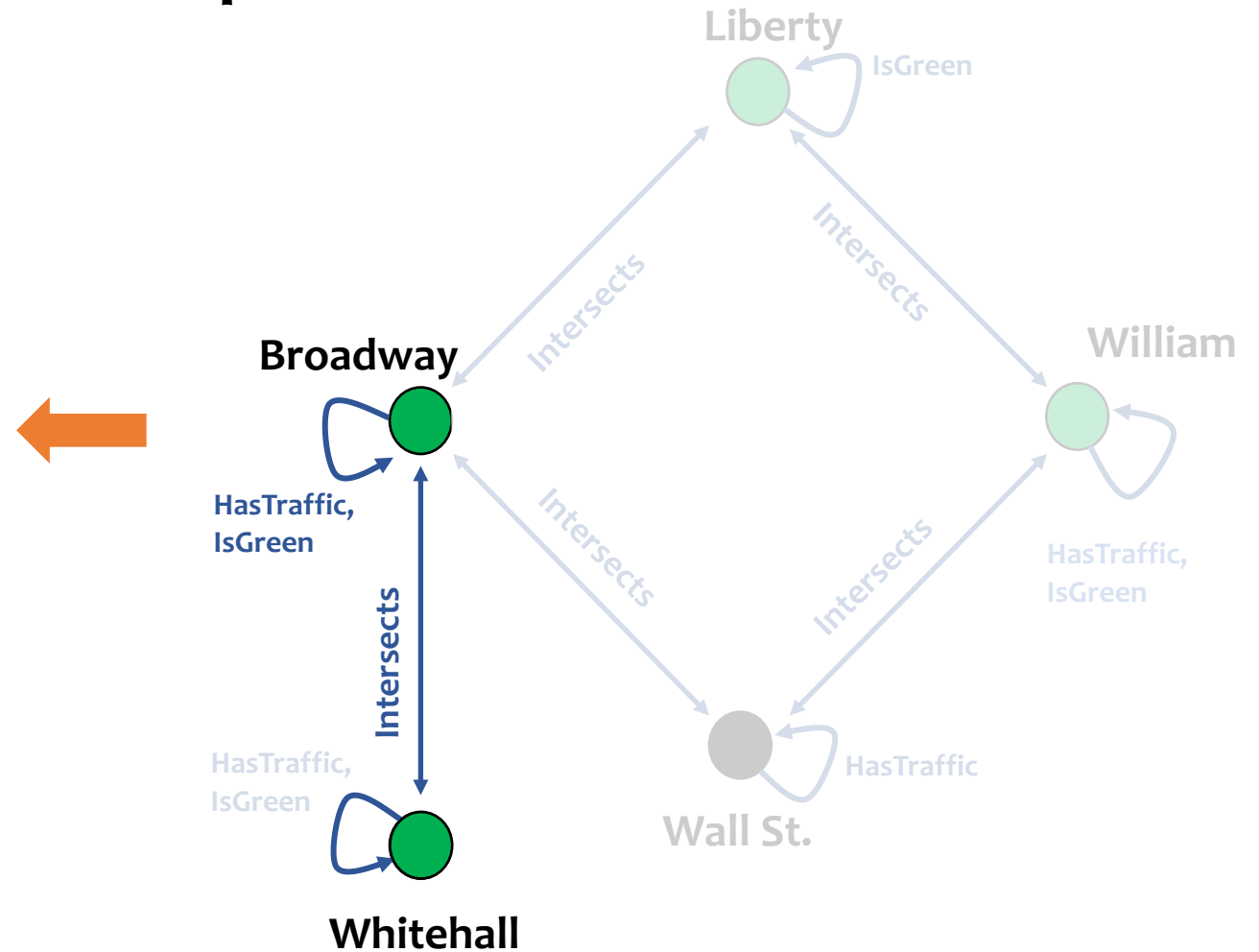
$\text{Crashes}(x) : \neg \text{HasTraffic}(x), \text{isGreen}(x), \text{Intersects}(x, y).$

## Crashes

Broadway

William St

Whitehall St





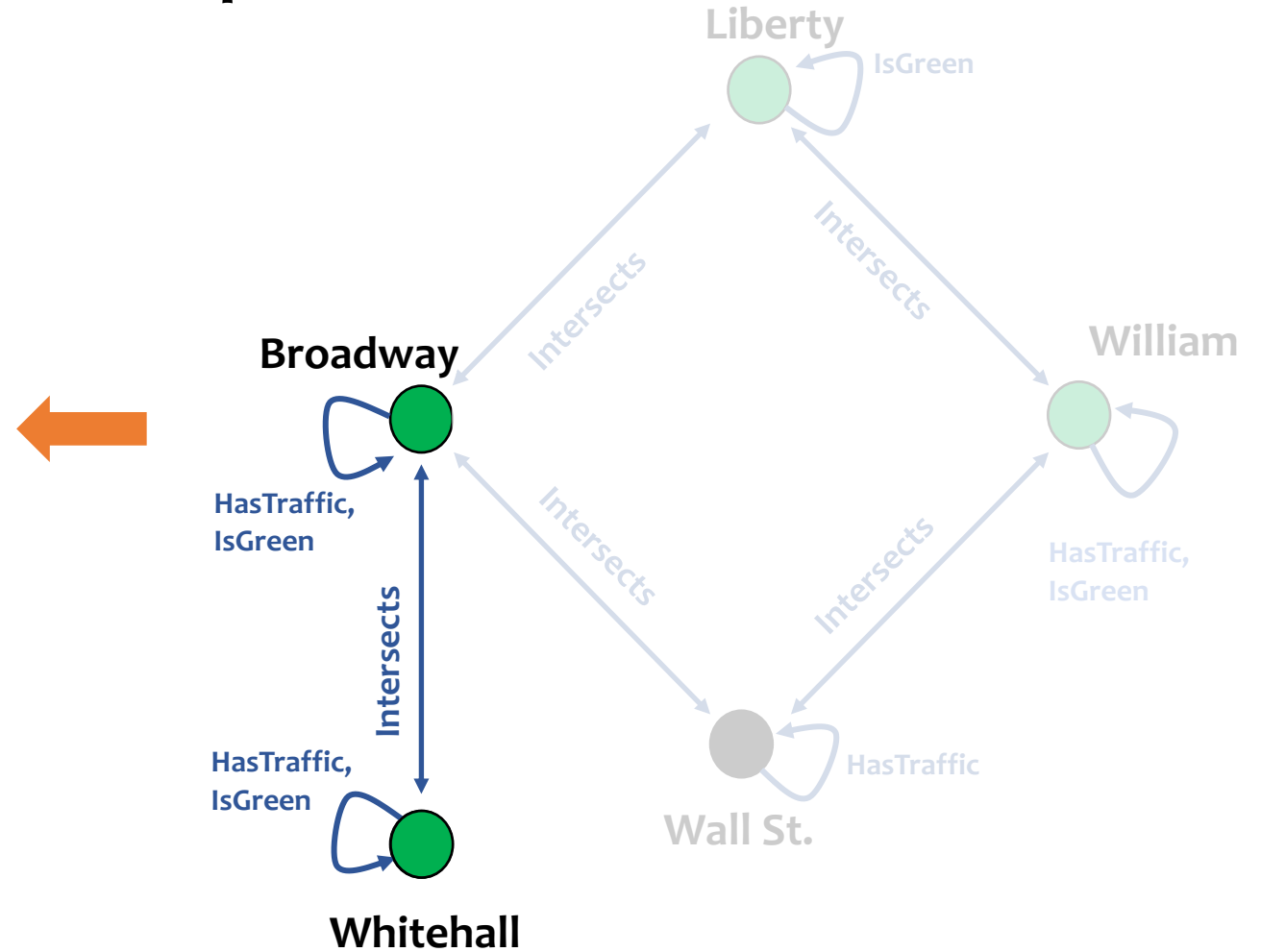
# An Example

## Crashes

Broadway

Whitehall St

$\text{Crashes}(x) : \neg \text{HasTraffic}(x), \text{isGreen}(x),$   
 $\text{Intersects}(x, y),$   
 $\text{HasTraffic}(y), \text{isGreen}(y).$



# An Example

## Crashes

Broadway

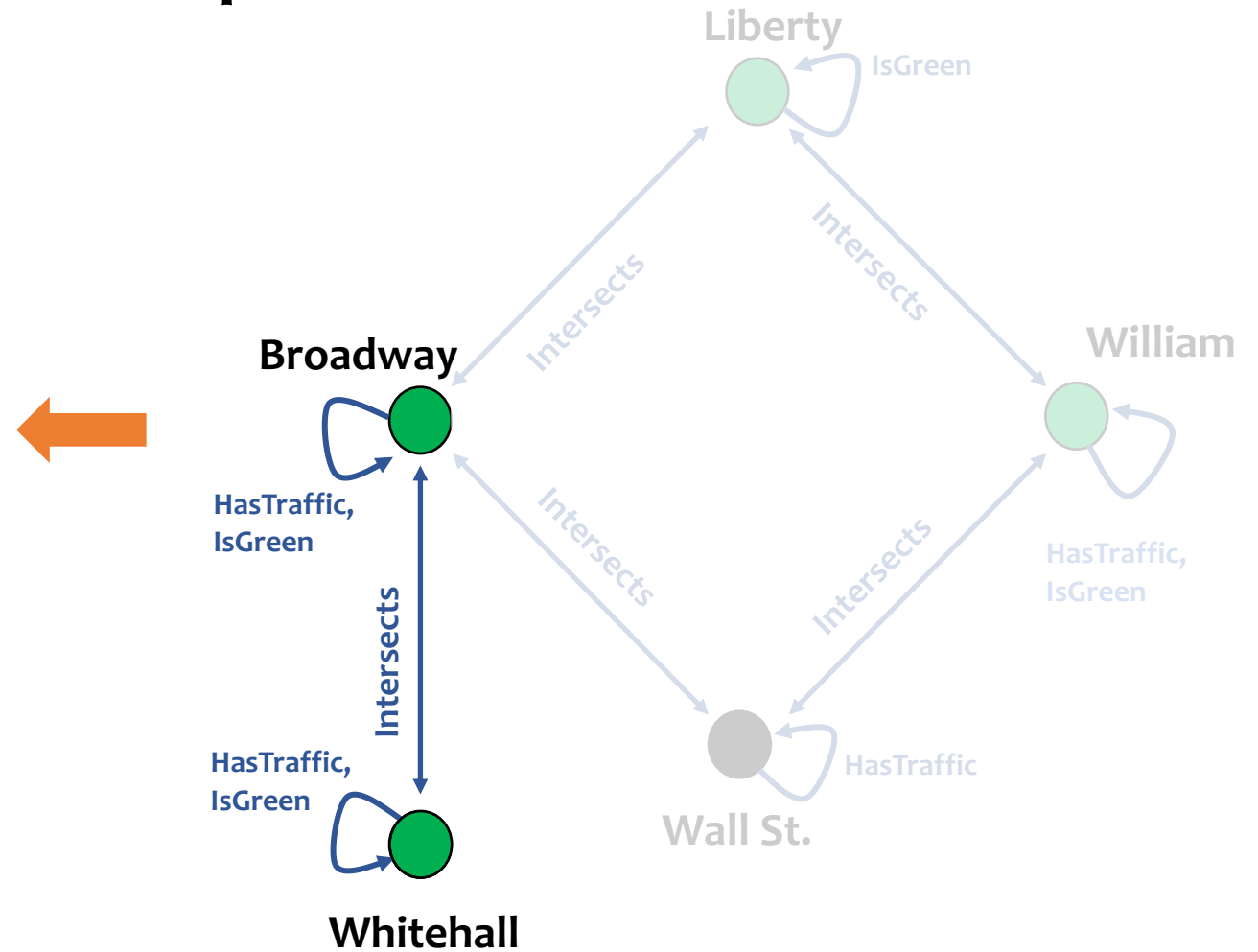
Whitehall St

$\text{Crashes}(x) : \neg \text{HasTraffic}(x), \text{isGreen}(x),$   
 $\text{Intersects}(x, y),$   
 $\text{HasTraffic}(y), \text{isGreen}(y).$

## Crashes

Broadway

Whitehall St



# An Example

## Crashes

Broadway

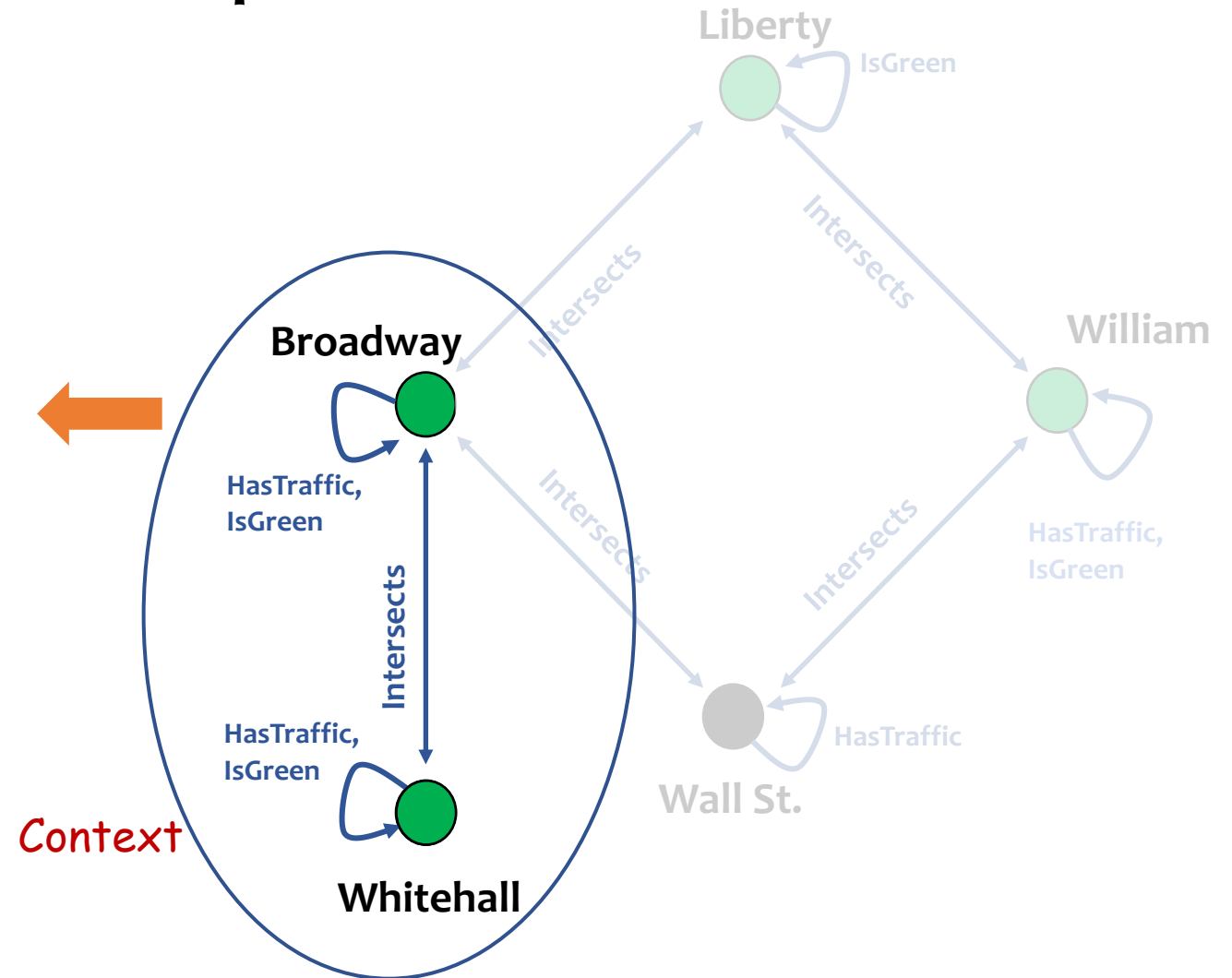
Whitehall St

$\text{Crashes}(x) : \neg \text{HasTraffic}(x), \text{isGreen}(x),$   
 $\text{Intersects}(x, y),$   
 $\text{HasTraffic}(y), \text{isGreen}(y).$

## Crashes

Broadway

Whitehall St



# Guarantees

1. EGS is **terminating** as there are finitely many subgraphs.
2. EGS is **sound** because consistency is verified as a part of synthesis.
3. EGS is **complete** because:  
the query corresponding to the entire graph is consistent with the examples if and only if some consistent query exists.

# Complexity of Relational Query Synthesis

Aalok Thakkar, Rajeev Alur, Mayur Naik  
University of Pennsylvania, Philadelphia, USA  
{athakkar,alur,mhnaik}@cis.upenn.edu

## 1 INTRODUCTION

The synthesis of relational queries from input-output examples has been studied in the context of inductive logic programming [2, 4, 6–8], program synthesis [5, 9, 11–14], and neural learning [10]. It is a challenging problem, and analyzing the computational complexity of the problem for even restricted fragments can significantly impact the development of synthesis tools.

For instance, several tools use language biases such as mode declarations, templates, meta-rules, and candidate rules to constraint the space of candidate programs [4, 6, 7, 9, 11]. Studying the hardness of the problem can allow us to determine bounds on the language biases such that completeness of the search process is not compromised. Tools that search through an infinite space do not terminate if the instance of the synthesis problem is *unrealizable* [5, 14]. Studying the unrealizability of the problem instance can help determine when such a search is futile and should be abandoned, allowing us to give termination guarantees for these tools.

The above mentioned synthesis tools consider different frag-

predicate  $R$  with a list of  $k$  variables. Then, a rule  $r$  is of the form:

$$R_h(\vec{u}_h) :- R_1(\vec{u}_1), R_2(\vec{u}_2), \dots, R_n(\vec{u}_n),$$

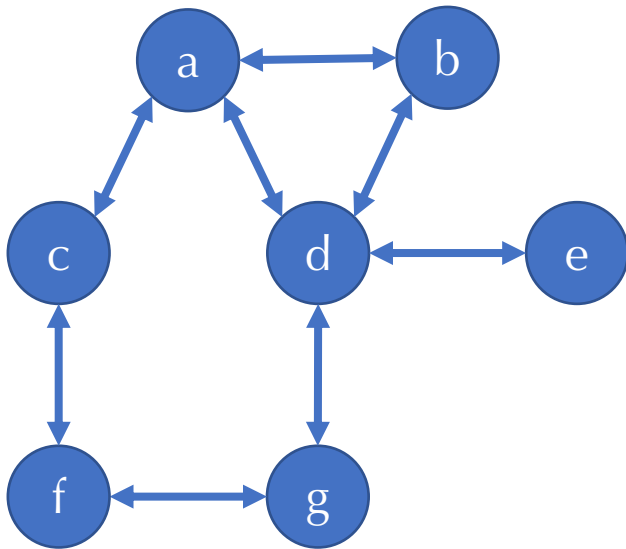
where the single literal on the left,  $R_h(\vec{u}_h)$ , is the *head* of  $r$  and  $R_1(\vec{u}_1), R_2(\vec{u}_2), \dots, R_n(\vec{u}_n)$ , is called the *body* of  $r$ . The literals in the body can have input predicates, invented predicates, or output predicates, while the head of the rules must have either invented predicates or output predicates. A variable that occurs in the head must appear at least once in the body to bound the variables. The size of a rule is defined as the number of literals in its body.  $|P|$ , the size of a query  $P$ , is defined as the sum of the size of rules in its body.

A fragment of these queries called *union of conjunctive queries* (UCQ) is of interest in Section 4. A UCQ consists of rules where the body of the rule comprises only of input predicates. UCQ is equivalent to select-project-join queries in relational algebra [3].

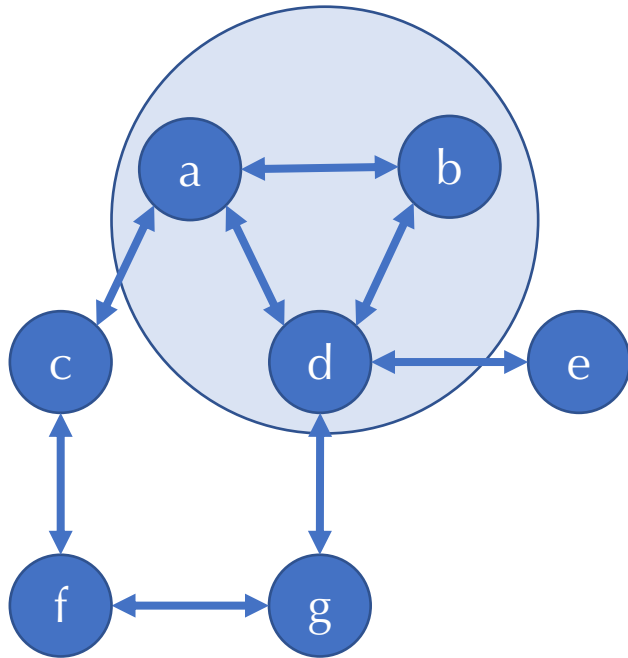
# Decidability and Complexity

The instance of the synthesis problem is realizable if and only if the query corresponding to the **entire constant co-occurrence graph** is consistent with the input-output examples.

# Hardness Result

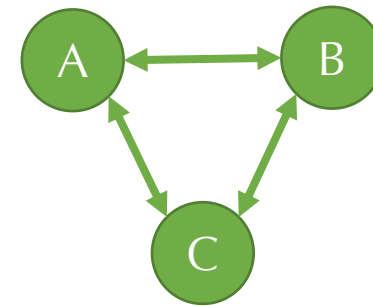
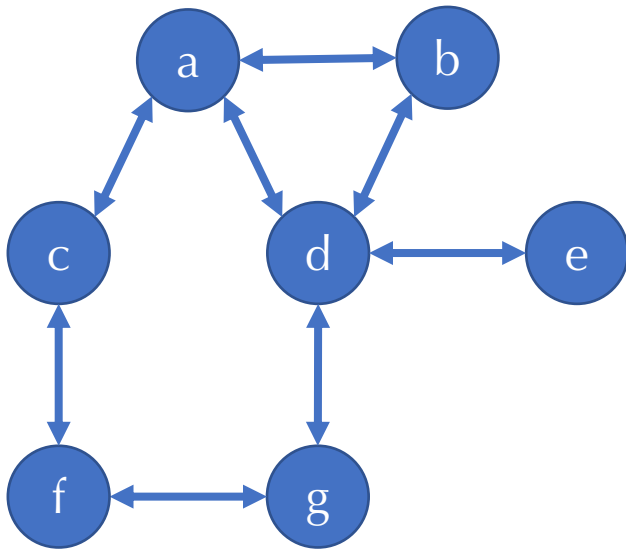


# Hardness Result

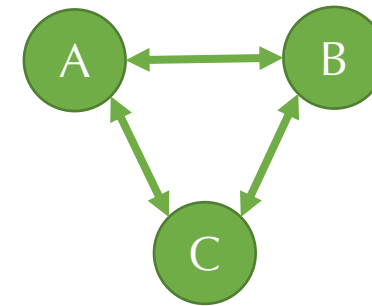
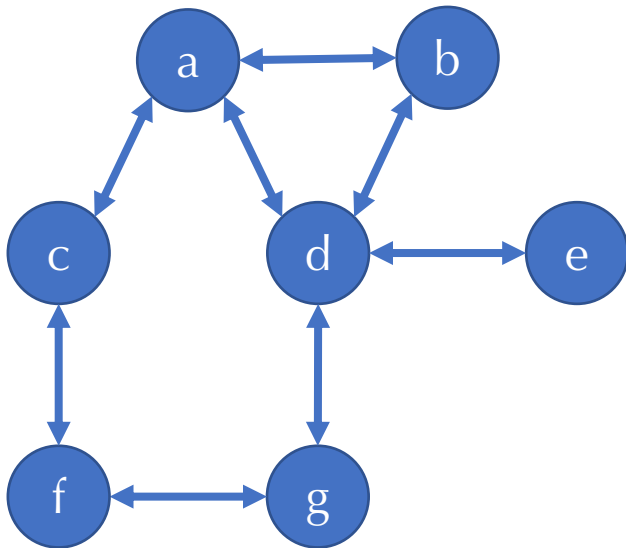




# Hardness Result



# Hardness Result



Target
A
B
C

# Completeness Guarantees

The instance of the synthesis problem is realizable if and only if there exists a query of size at most  $|I \times O^+|$  that is consistent with the examples.

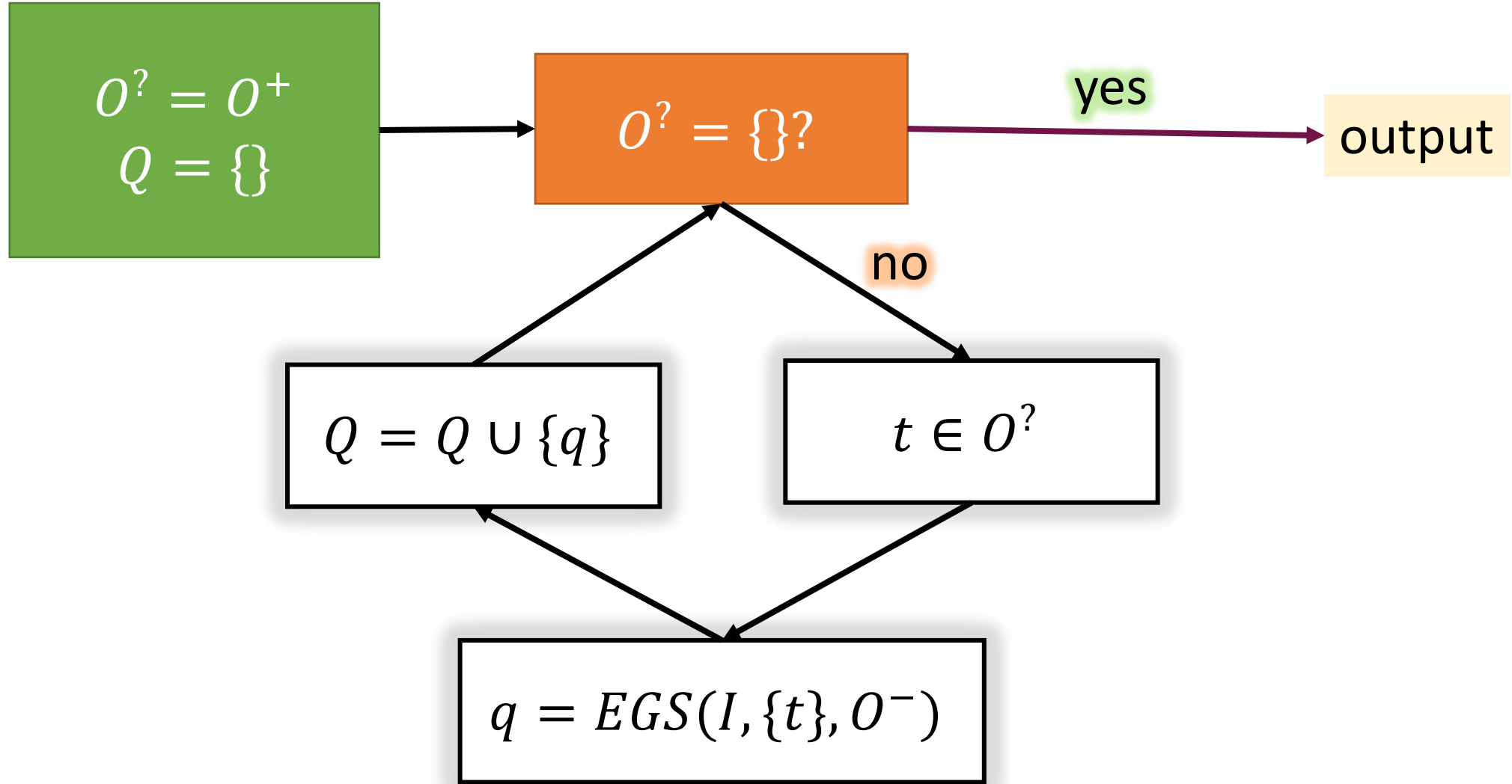
# Extensions

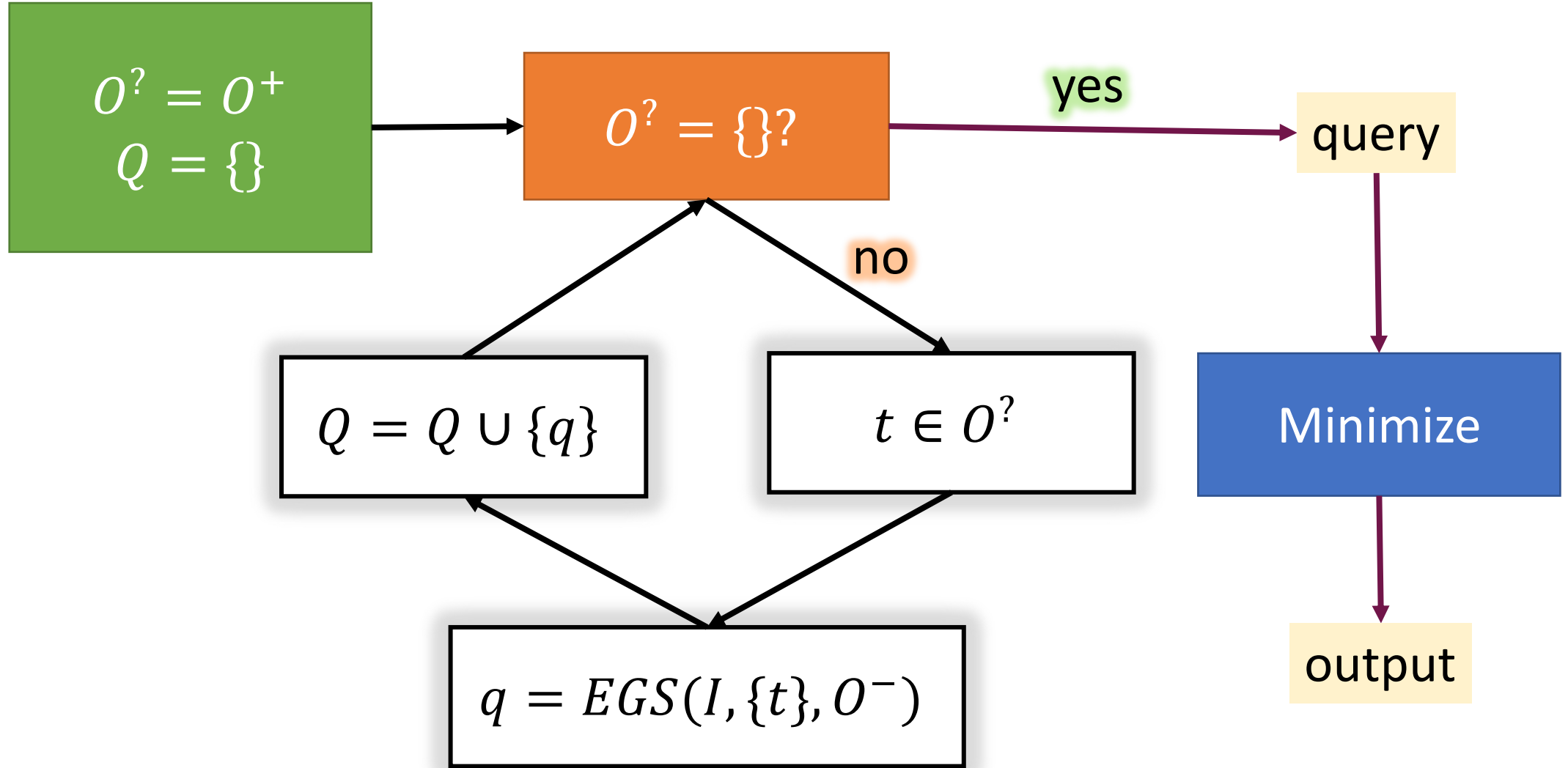


Union

Recursion

Comparison Predicates





# Extensions



Union

Recursion

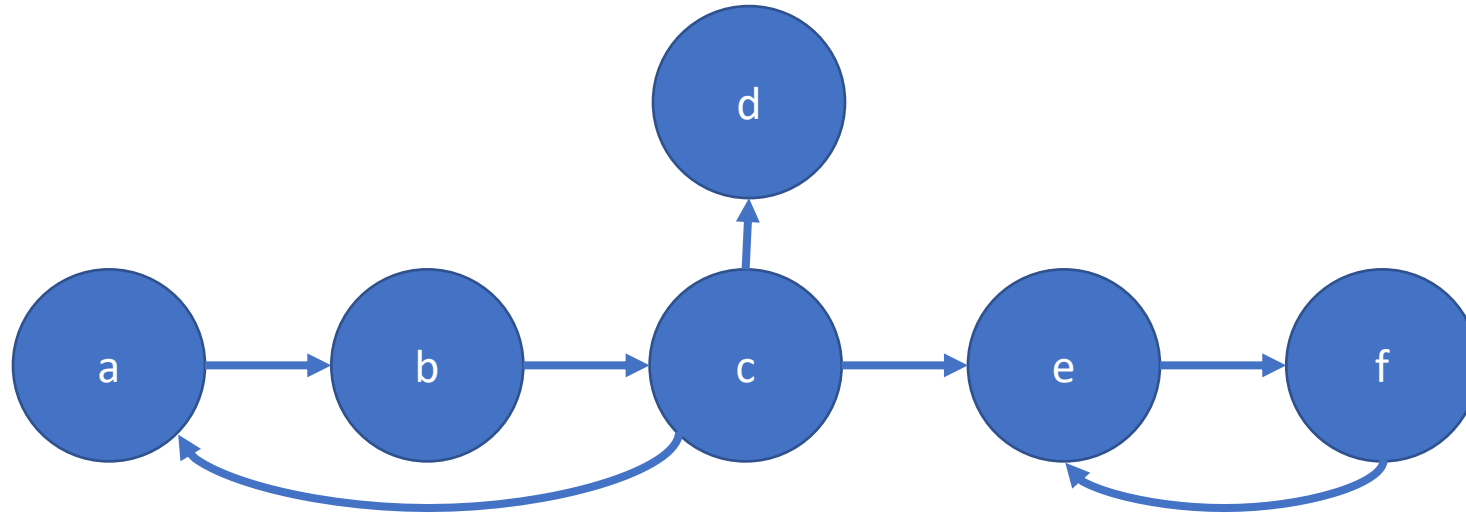
Comparison Predicates

$\text{scc}(x, y) : \neg \text{path}(x, y), \text{path}(y, x).$

$\text{path}(x, y) : \neg \text{edge}(x, y).$

$\text{path}(x, y) : \neg \text{egde}(x, y), \text{egde}(y, z).$

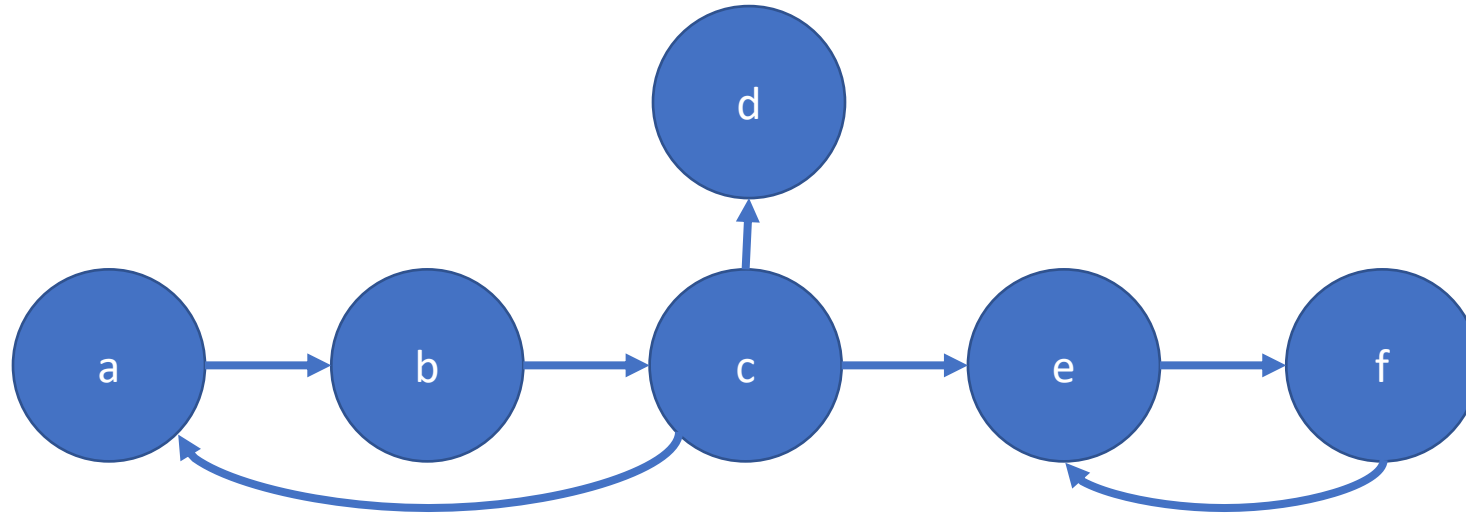




$\text{scc}(x, y) : - \text{path}(x, y), \text{path}(y, x).$

$\text{path}(x, y) : - \text{edge}(x, y).$

$\text{path}(x, y) : - \text{path}(x, z), \text{path}(z, y).$



$\text{scc}(x, y) : - \text{edge}(x, y), \text{edge}(y, x).$

$\text{scc}(x, y) : - \text{edge}(x, y), \text{edge}(y, z), \text{edge}(z, x).$

$\text{scc}(x, z) : - \text{edge}(x, y), \text{edge}(y, z), \text{edge}(z, x).$

# Normalization

$\text{scc}(x, y) : - \text{edge}(x, y), \text{edge}(y, x).$

$\text{scc}(x, y) : - \text{edge}(x, y), \text{edge}(y, z), \text{edge}(z, x).$

$\text{scc}(x, z) : - \text{edge}(x, y), \text{edge}(y, z), \text{edge}(z, x).$

# Normalization

$\text{scc}(x, y) : \neg R(x, y), R(y, x).$

$\text{scc}(x, y) : \neg R(x, y), R(y, z), R(z, x).$

$\text{scc}(x, z) : \neg R(x, y), R(y, z), R(z, x).$

$R(x, y) : \neg \text{edge}(x, y).$

# Normalization

$\text{scc}(x, y) : \neg R(x, y), R(y, x).$

$\text{scc}(x, y) : \neg R(x, y), S(y, x).$

$\text{scc}(x, z) : \neg S(x, z), R(z, x).$

$R(x, y) : \neg \text{edge}(x, y).$

$S(x, z) : \neg R(x, y), R(y, z).$

# Normalization

$\text{scc}(x, y) : \neg R(x, y), R(y, x).$

$\text{scc}(x, y) : \neg S(x, z), R(z, x).$

$\text{scc}(x, z) : \neg S(x, z), R(z, x).$

$R(x, y) : \neg \text{edge}(x, y).$

$S(x, z) : \neg R(x, y), R(y, z).$

# Unification

$\text{scc}(x, y) : \neg P(x, y), P(y, x).$

$\text{scc}(x, y) : \neg P(x, y), P(z, y).$

$\text{scc}(x, z) : \neg P(x, z), P(z, x).$

$P(x, y) : \neg \text{edge}(x, y).$

$P(x, z) : \neg P(x, y), P(y, z).$

# Unification

$\text{scc}(x, y) : \neg P(x, y), P(y, x).$

$P(x, y) : \neg \text{edge}(x, y).$

$P(x, z) : \neg P(x, y), P(y, z).$



# Extensions



Union

Recursion

Comparison Predicates

```
SELECT registration.studentID
      FROM registration JOIN department
            ON registration.deptCode = department.deptCode
     WHERE registration.courseID < 500
            AND department.school = "Engineering"
```

```
SELECT registration.studentID  
      FROM registration JOIN department  
            ON registration.deptCode = department.deptCode
```

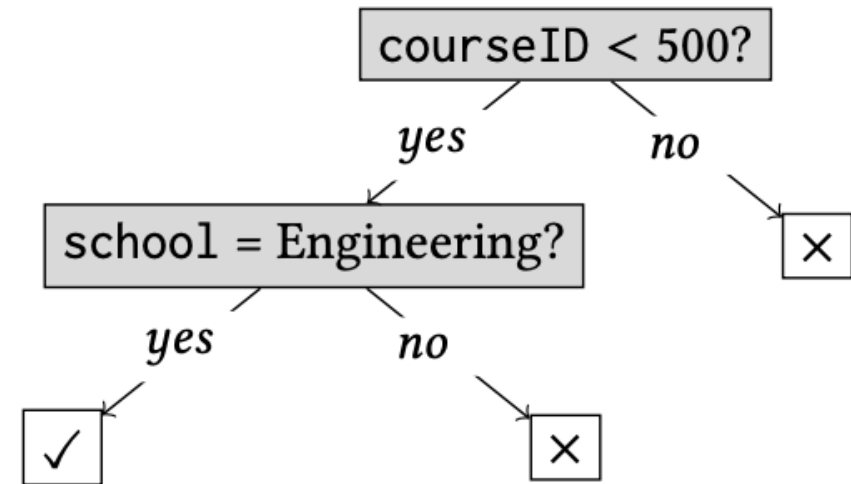
```
SELECT registration.studentID
      FROM registration JOIN department
            ON registration.deptCode = department.deptCode
     WHERE registration.courseID < 500
            AND department.school = "Engineering"
```

```

SELECT registration.studentID
      FROM registration JOIN department
            ON registration.deptCode = department.deptCode
      WHERE registration.courseID < 500
            AND department.school = "Engineering"

```

studentID	deptCode	courseID	school
Alice	Comp.	201	Engineering
Alice	Chem.	310	Arts and Science
Alice	Mech.	550	Engineering
Bob	Mech.	320	Engineering
Bob	Mech.	550	Engineering
Charlie	Chem.	310	Arts and Science
David	Comp.	500	Engineering
David	Mech.	502	Engineering
Erin	Chem.	310	Arts and Science



# Future Work

Comprehensive Evaluation

Application

Aggregation